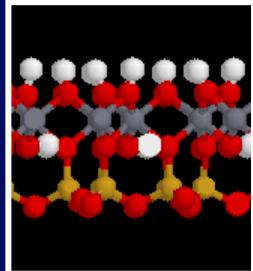


Integrated Ground Behavior

**Part A: Particle-level Phenomena & Macroscale
Behavior (J. Carlos Santamarina)**

Georgia Institute of Technology



fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness

soil

fine-grained soil fabric
coarse-grained soil packing
platy particles

conduction
diffusion
energy coupling

stiffness
threshold strain

strength
(scales)

rheology
diagenesis

fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
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forces
specific surface
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stiffness
threshold strain

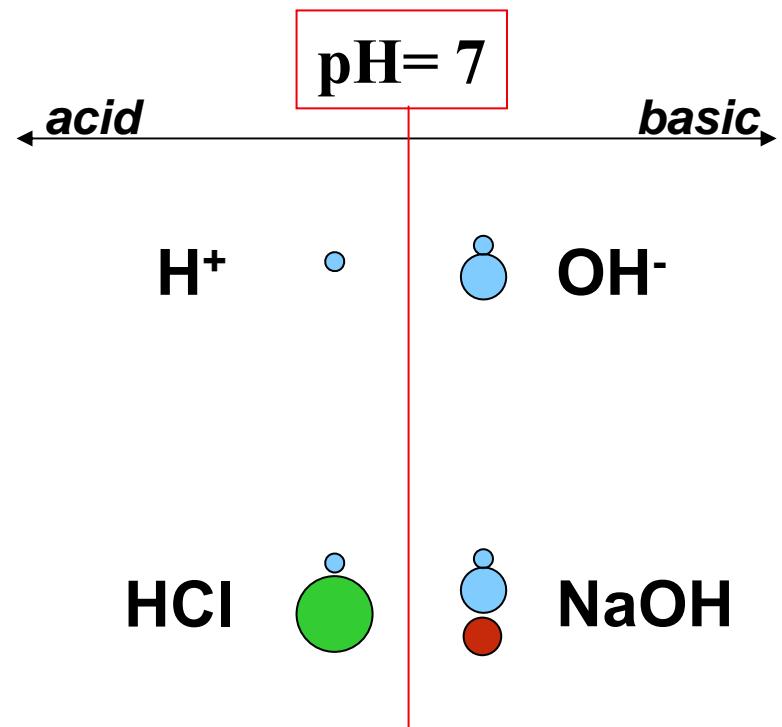
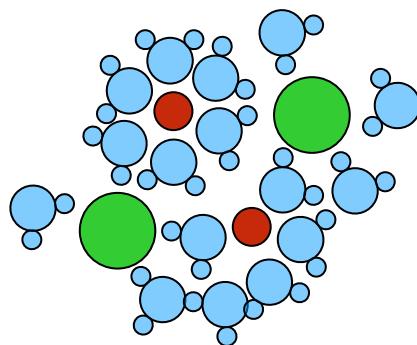
strength
(scales)

rheology
diagenesis

Water

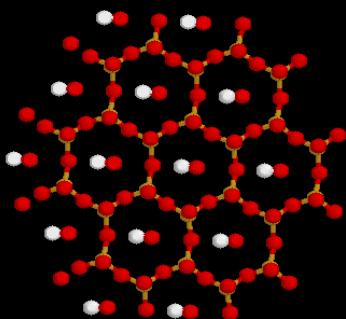
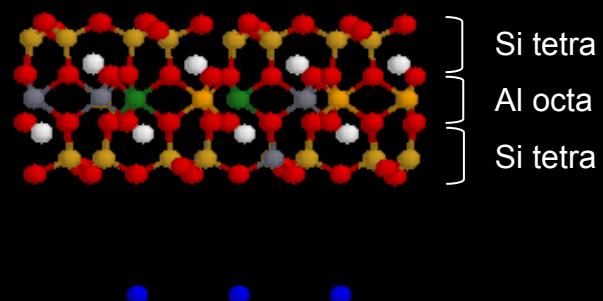
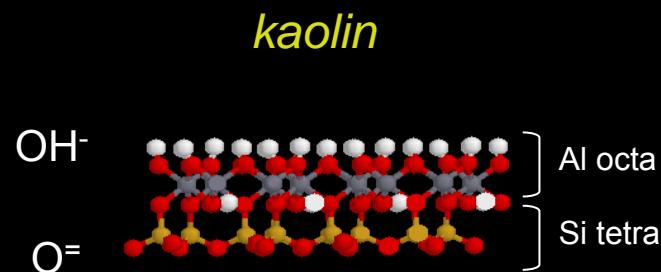


Ionic concentration

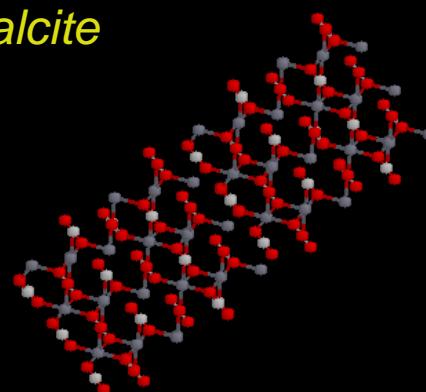


Minerals

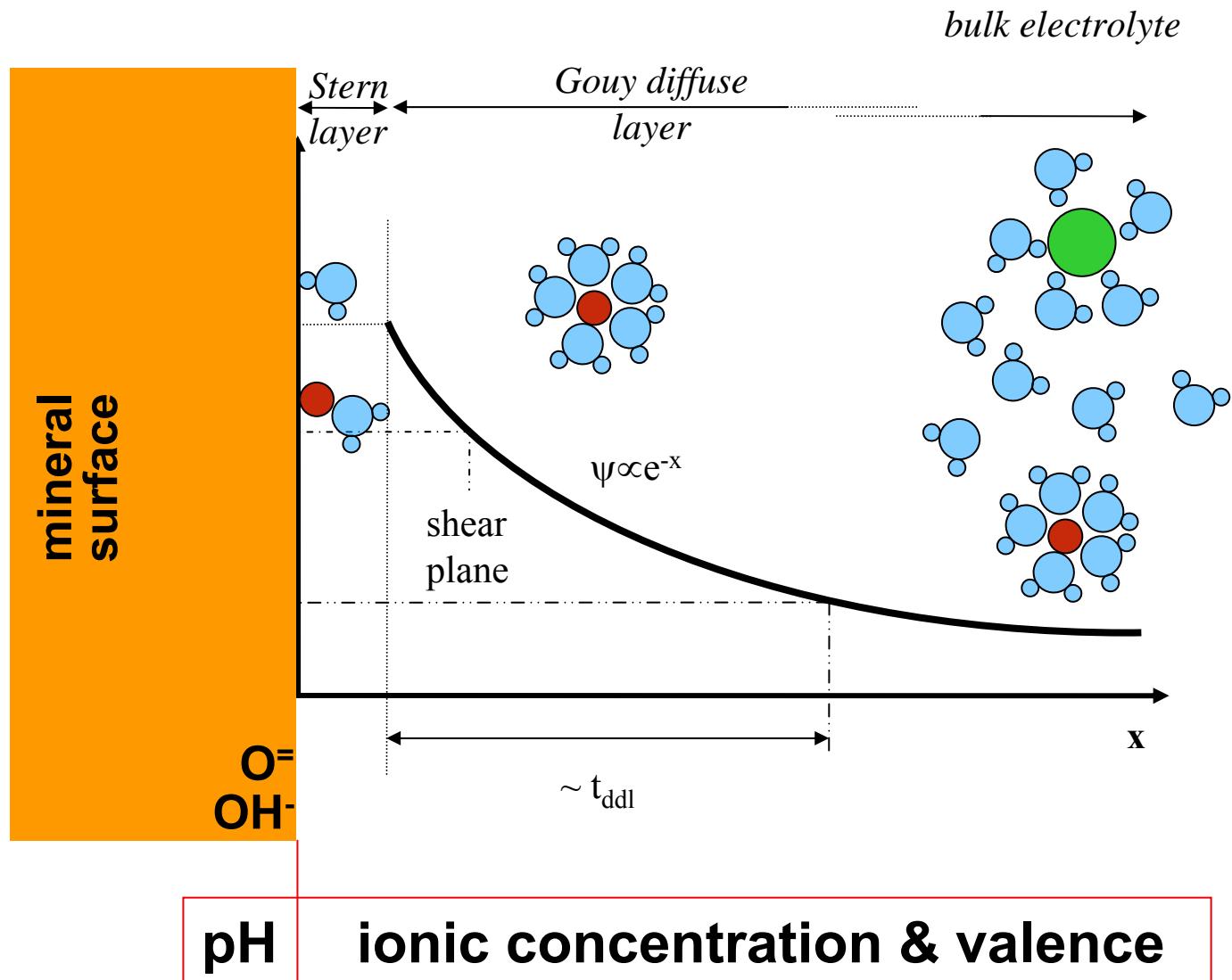
montmorillonite



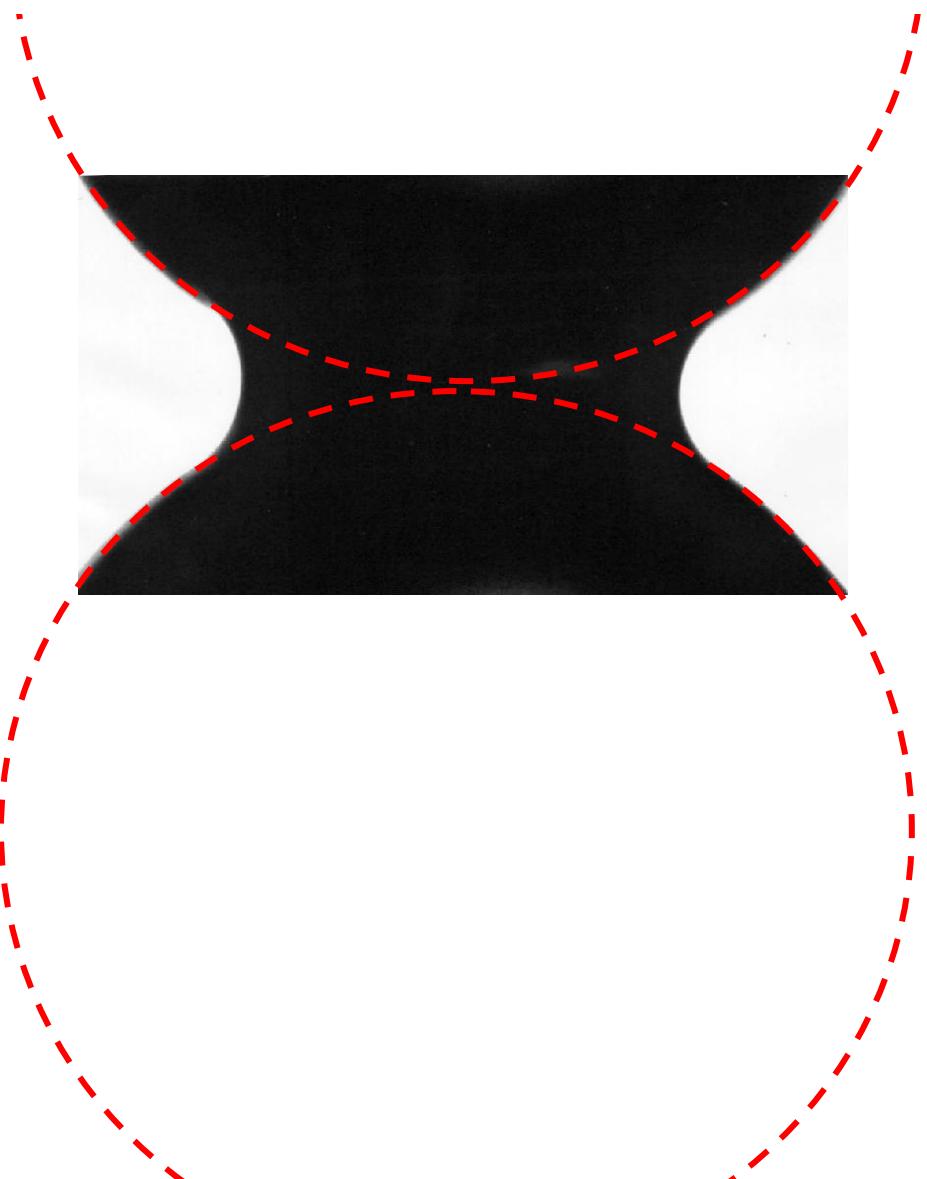
calcite



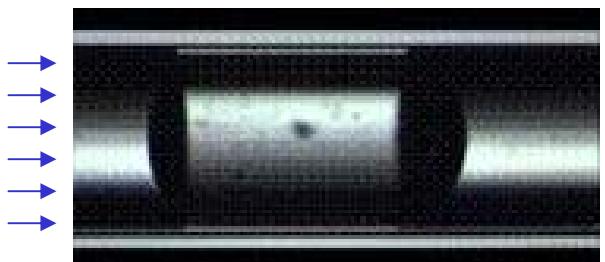
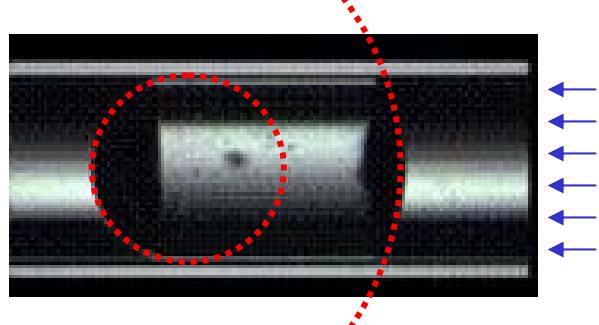
Diffuse double layer



Mixed fluid phase



Interacting menisci:



θ non-constant

fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness

soil

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Particle Forces

Skeletal

$$\underline{N} = \sigma' d^2$$

Weight

$$W = (\pi G_s \gamma_w / 6) d^3$$

Buoyant

$$U = (\pi \gamma_w / 6) d^3$$

Hydrodyn.

$$F_{\text{drag}} = 3\pi \mu v d$$

Capillary

$$F_{\text{cap}} = \pi T_s d$$

EI. attraction

$$\text{Att} = \frac{A_h}{24t^2} d$$

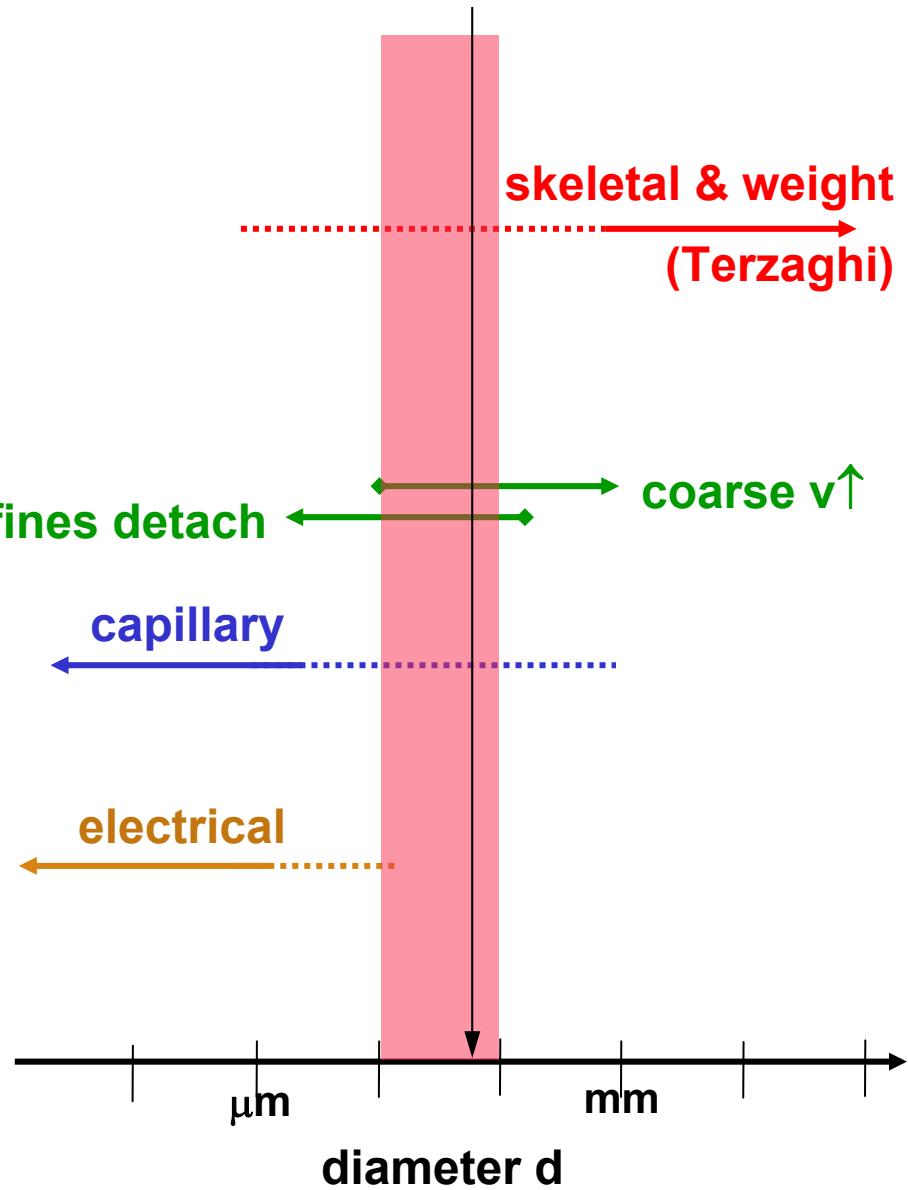
EI. repulsion

$$\text{Rep} = \frac{24\sqrt{c_o}}{10000} e^{-10^8 t \sqrt{c_o}} d$$

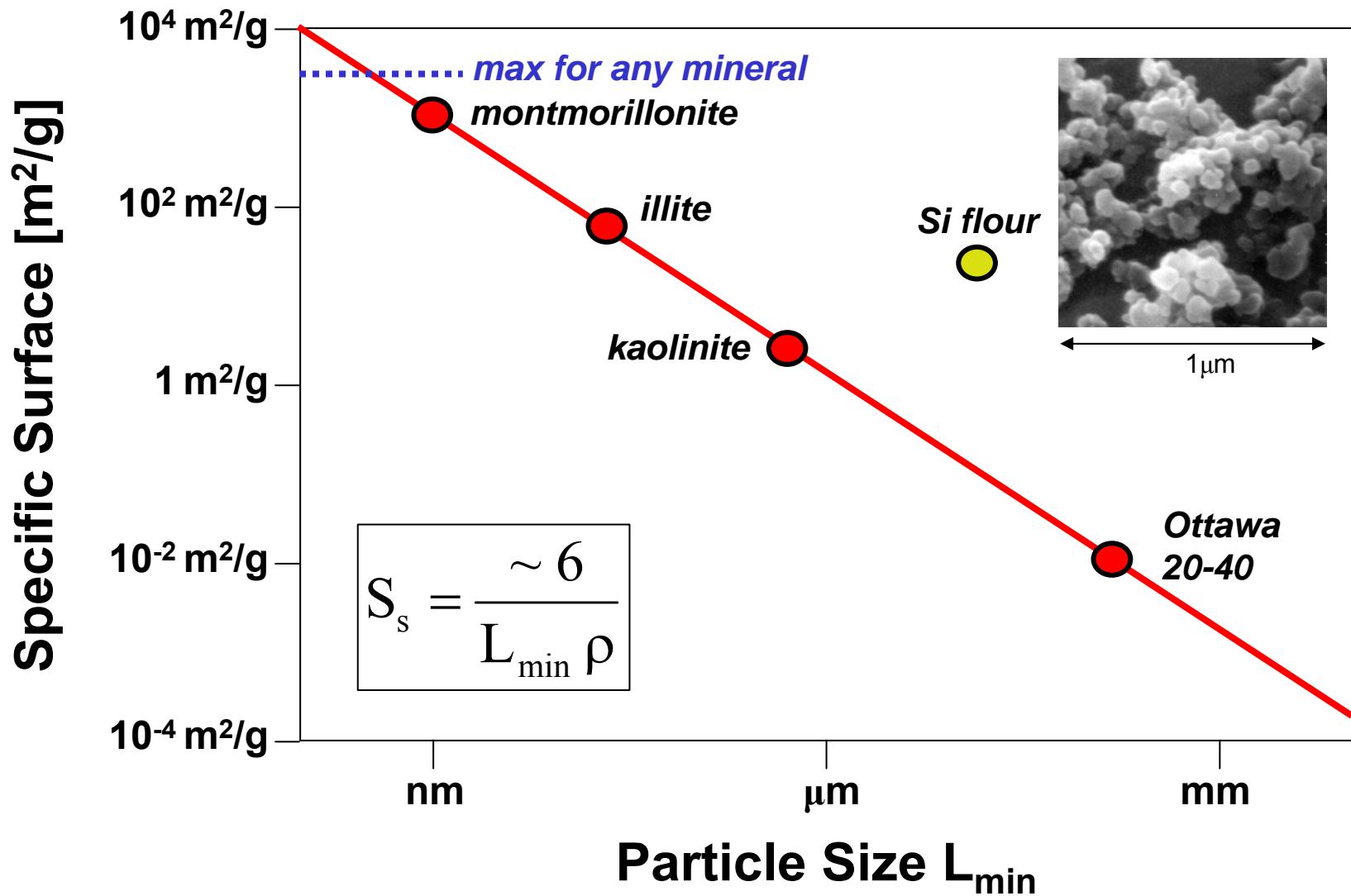
Cementation

$$T = \pi \sigma_{\text{ten}} t d$$

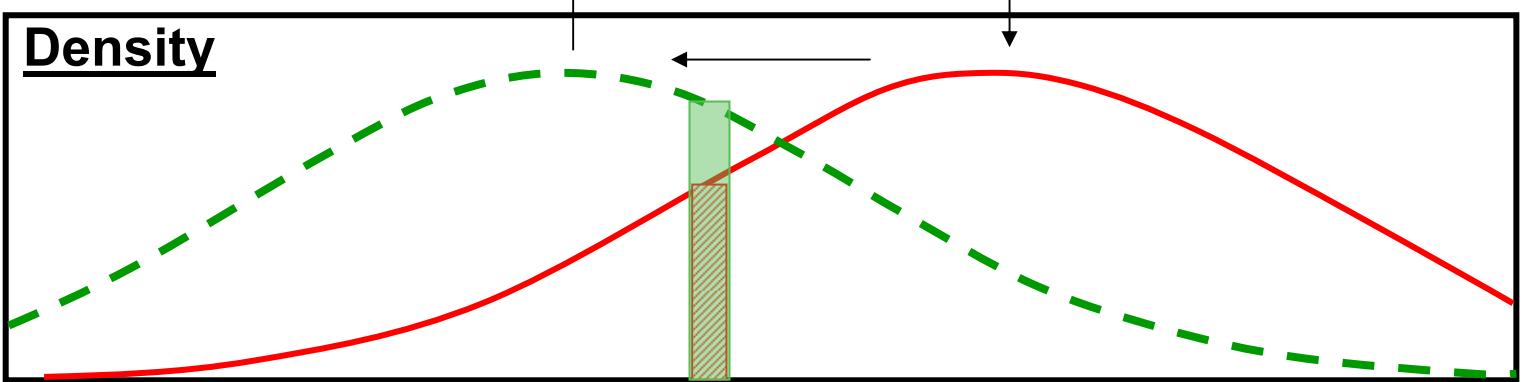
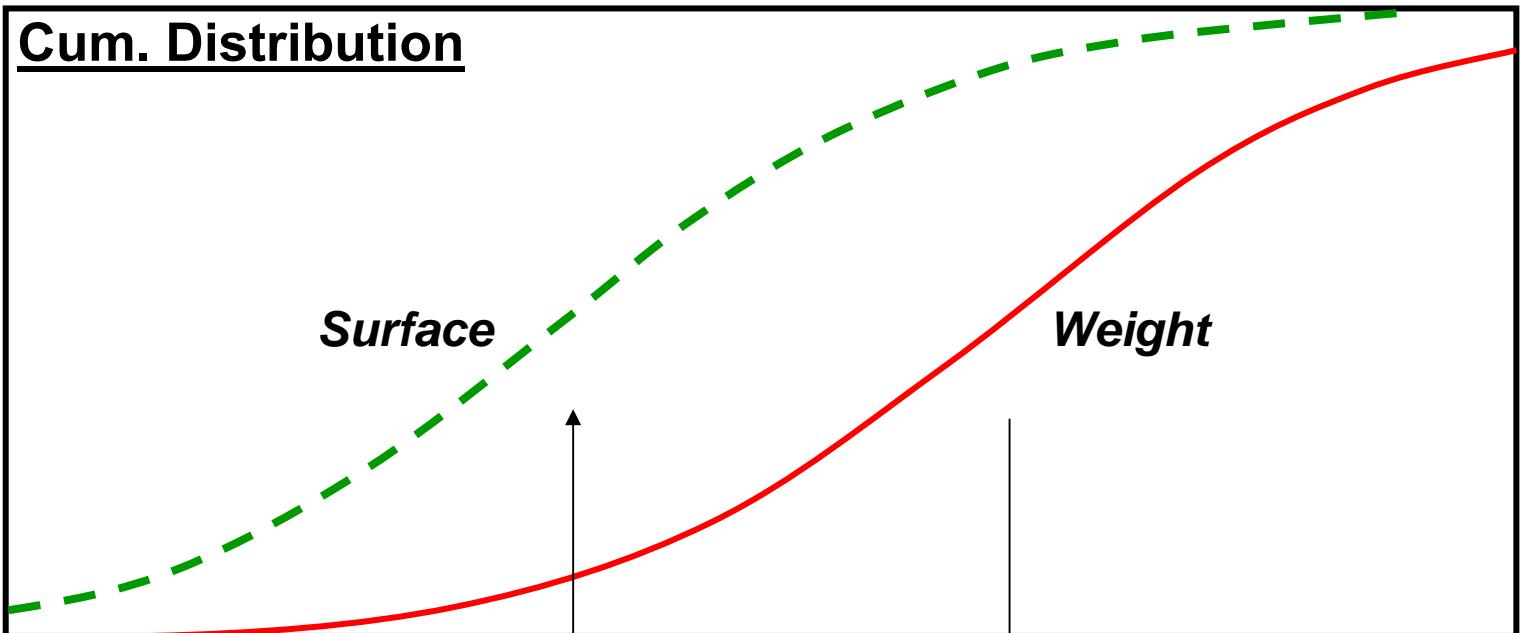
#200



Size and Surface - Surface Phenomena

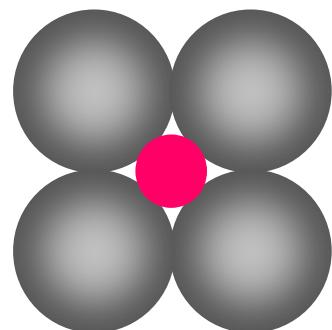


Size and Surface - Surface Phenomena

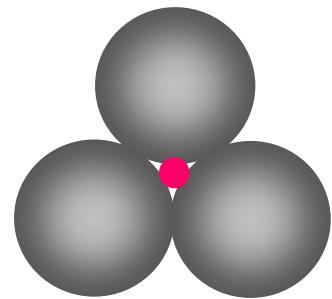


Grain size

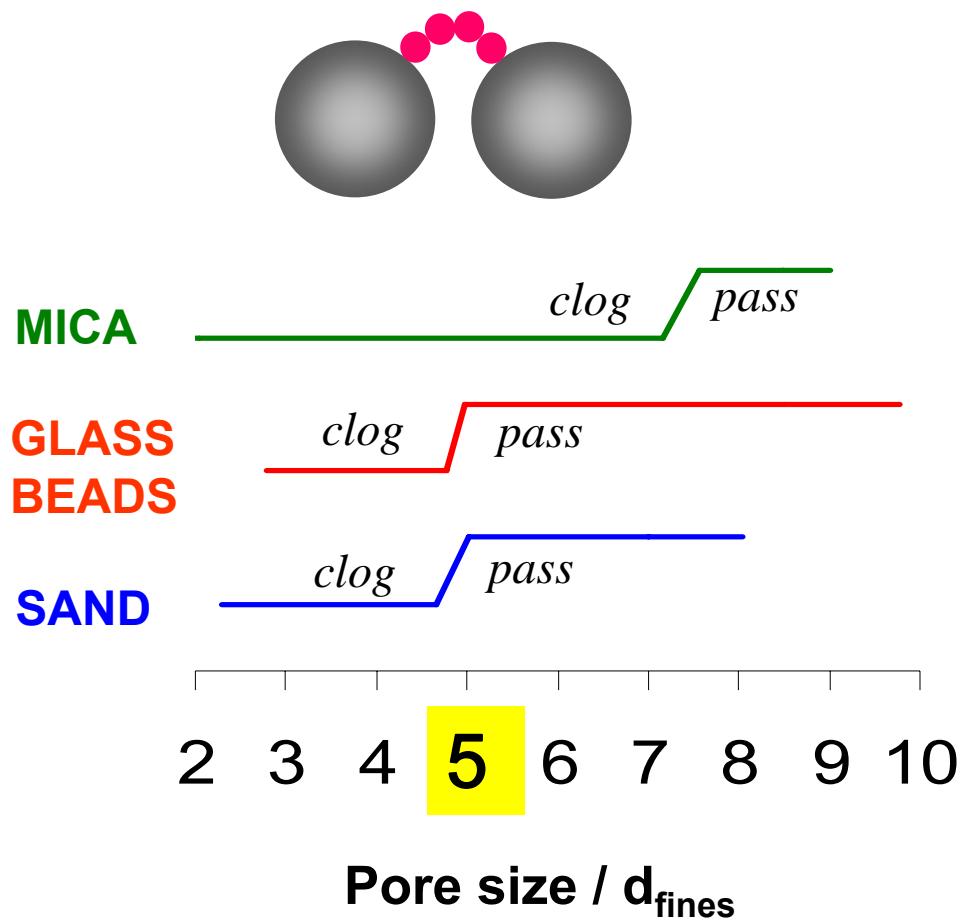
Fines migration and bridge formation



$D/d=2.4$



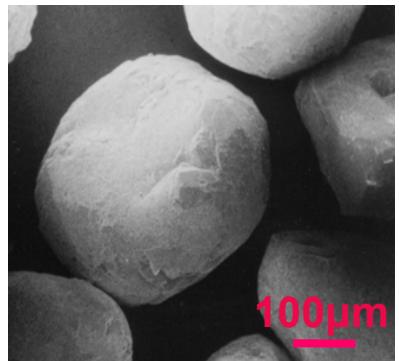
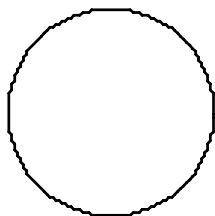
$D/d=6.5$



Pore size / d_{fines}

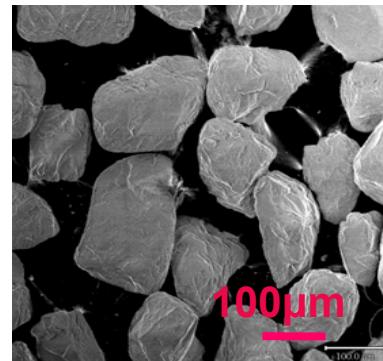
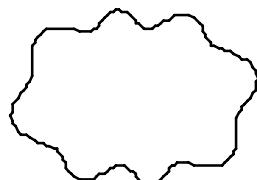
Particle Shape

sphericity
vs. ellipticity..platiness



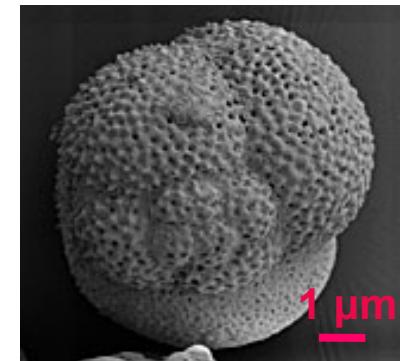
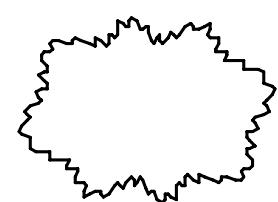
Ottawa

roundness
vs. angularity



Nevada

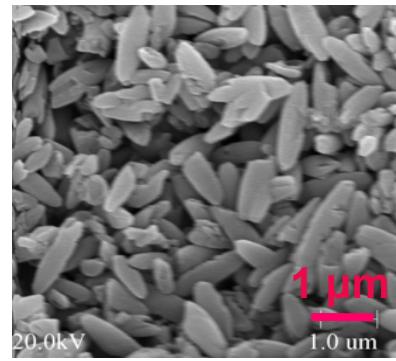
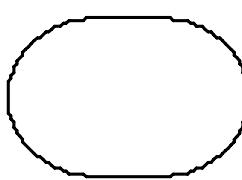
smoothness
vs. roughness



formineferan

sphericity

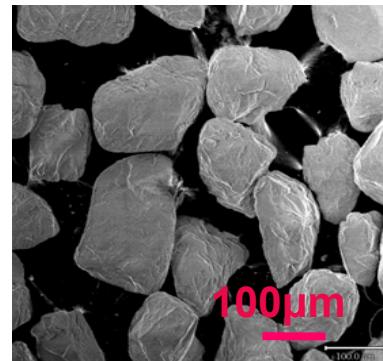
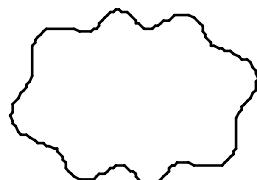
vs. ellipticity..platiness



PCC

roundness

vs. angularity

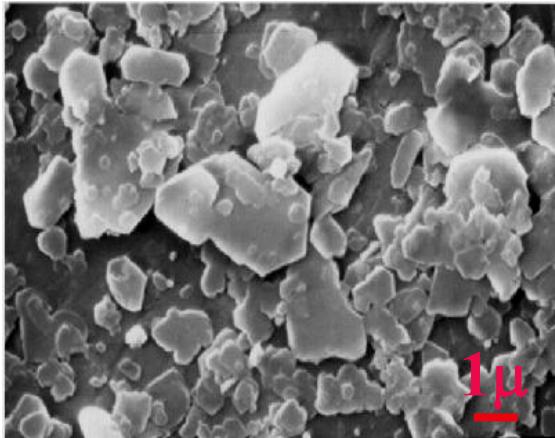


Ottawa

Particle Shape

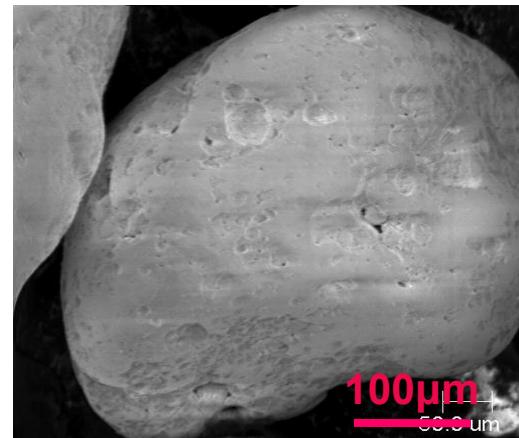
50 μm

chemically controlled



kaolinite

mechanically controlled



Margaret River

fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness

soil

fine-grained soil fabric
coarse-grained soil packing
platy particles

conduction
diffusion
energy coupling

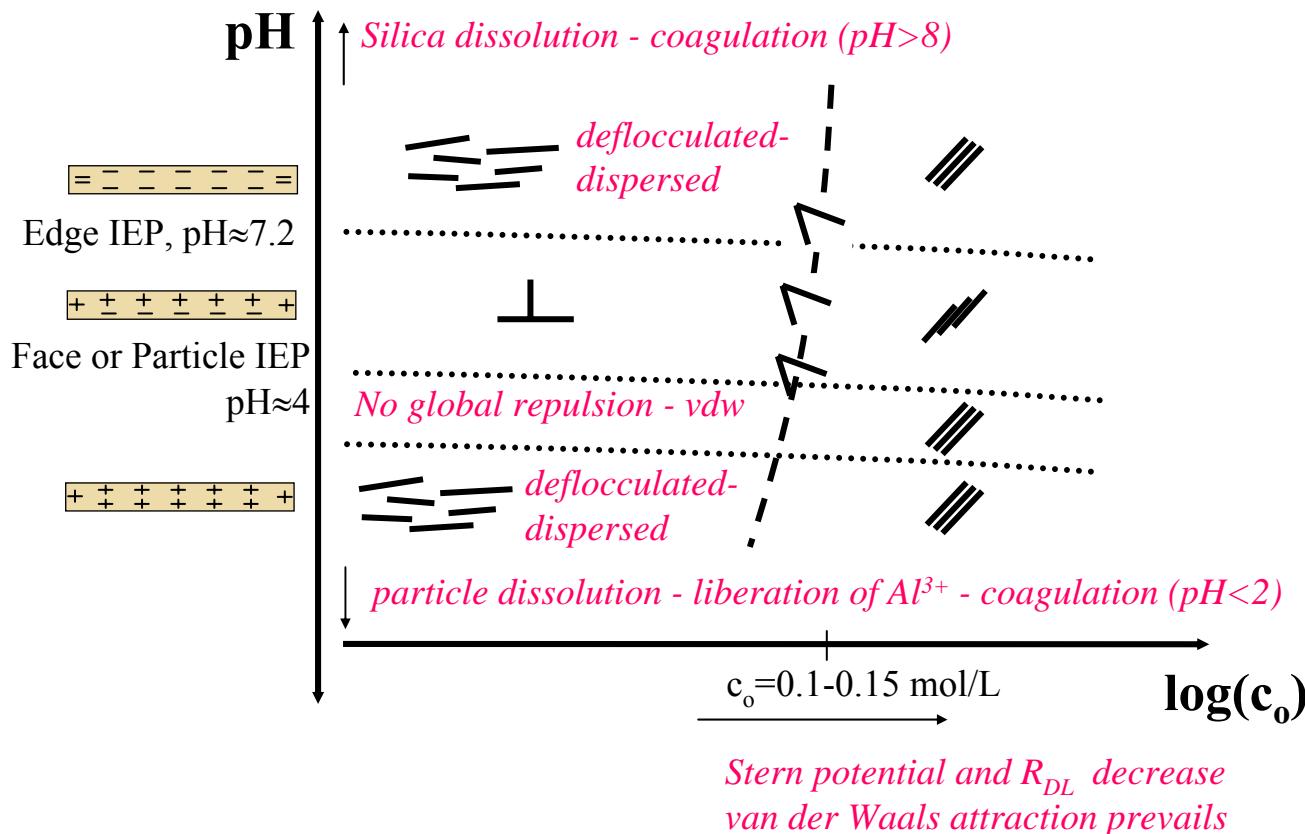
stiffness
threshold strain

strength
(scales)

rheology
diagenesis

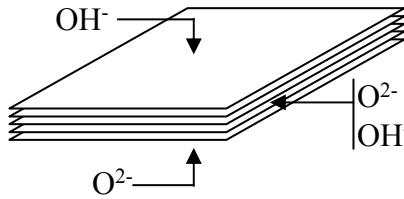
Fabric map

kaolinite

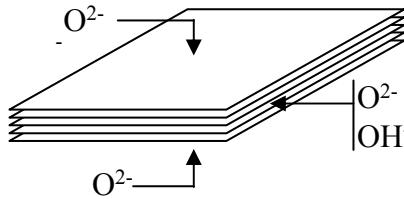


Clay minerals – Differences

1:1



2:1

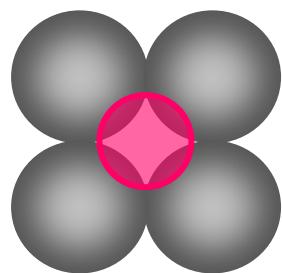


**different faces
different from edge**

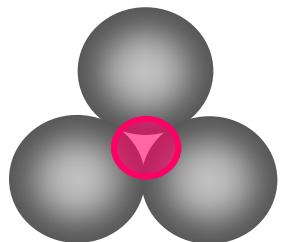
**edge contribution
charge change**

**ζ / particle thickness
hiding edge DL**

Coarse particles: relative size

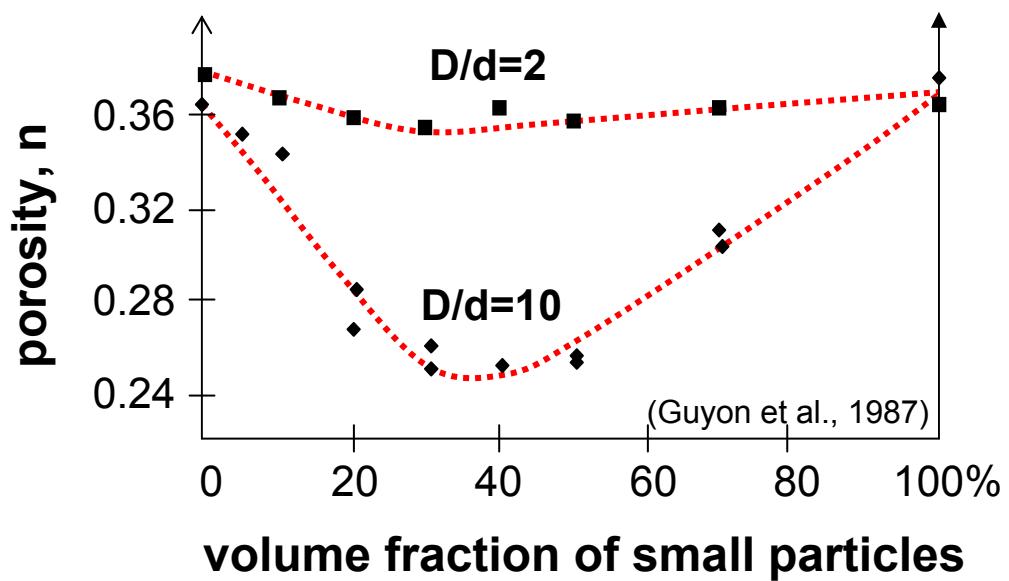


$D/d=1.37$



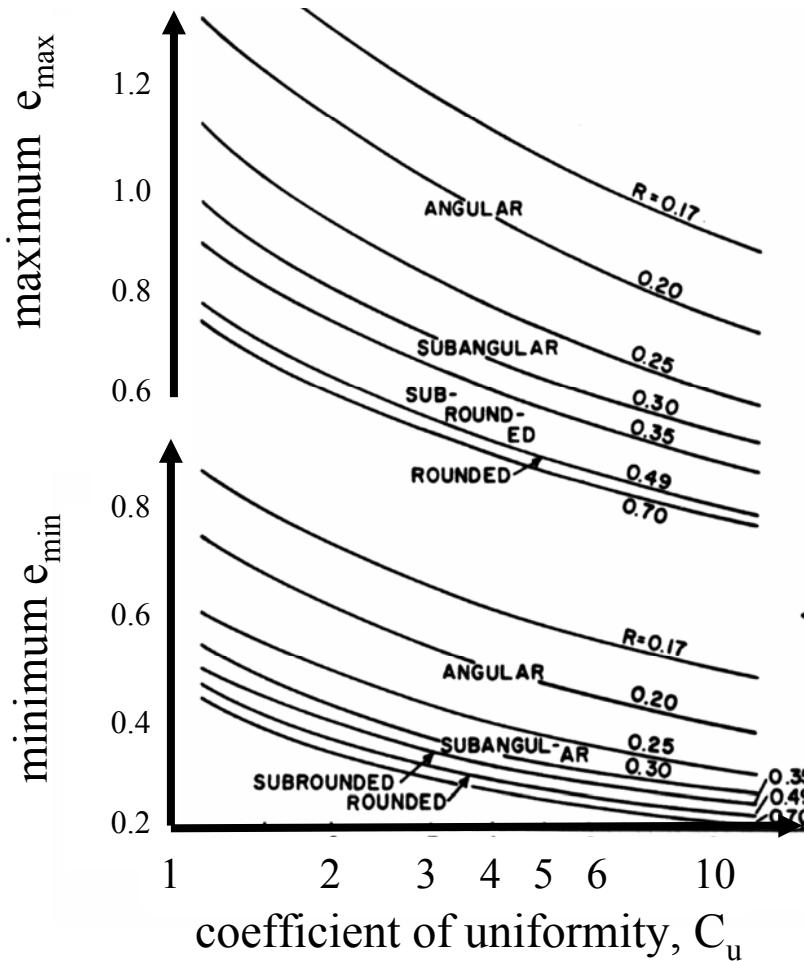
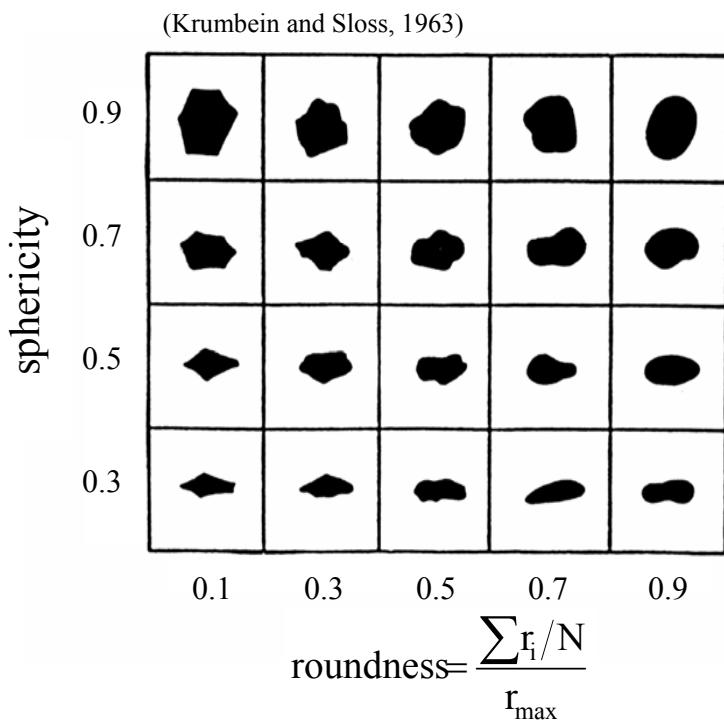
$D/d=5.3$

random packing:



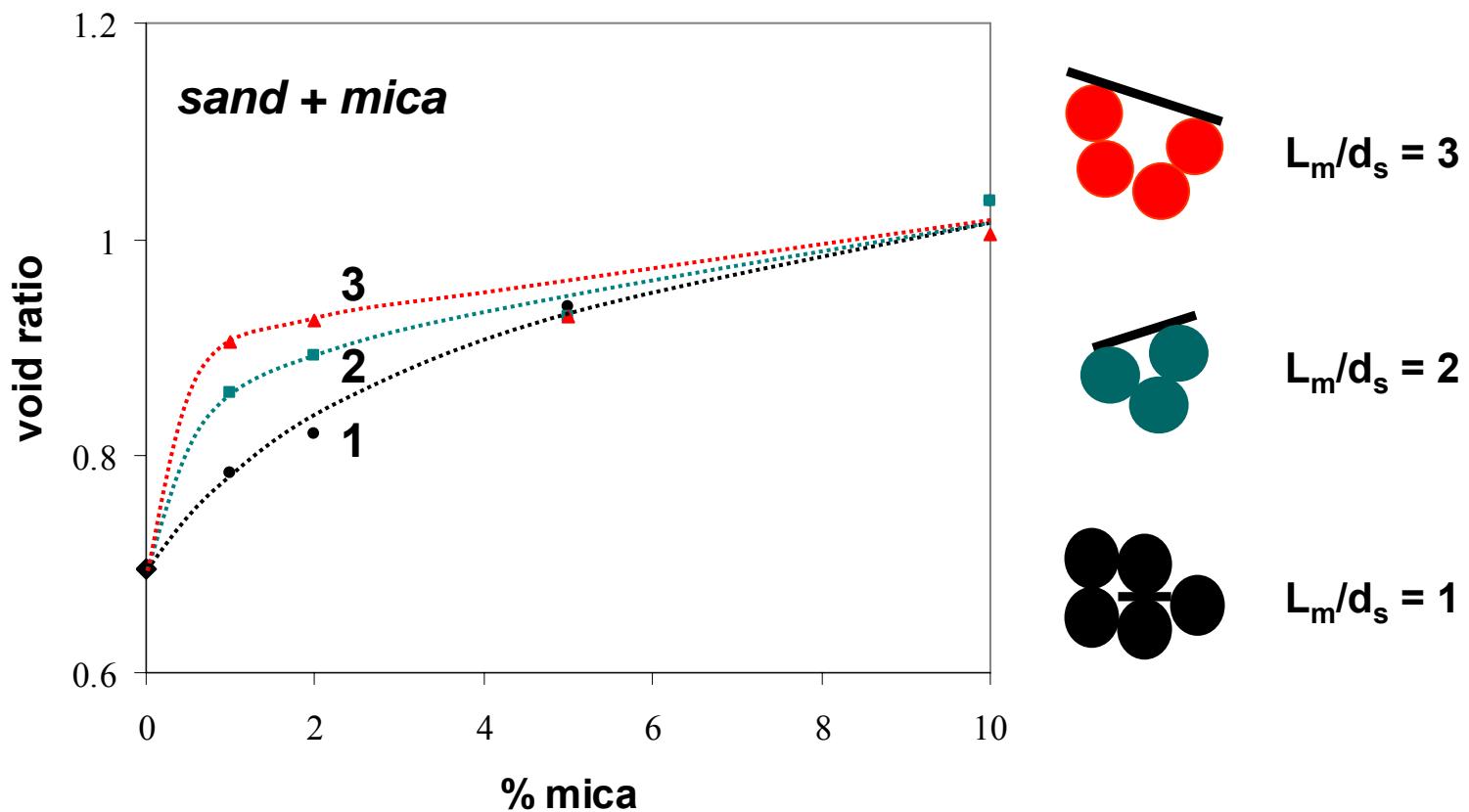
and...

Relative size and shape



(Youd, 1973; see also Maeda, 2001)

Platy particles: bridging



fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness

soil

fine-grained soil fabric
coarse-grained soil packing
platy particles

conduction
diffusion
energy coupling

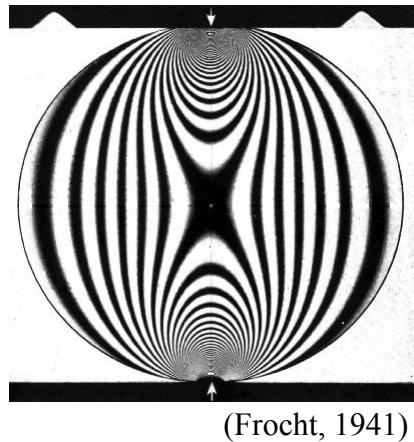
stiffness
threshold strain

strength
(scales)

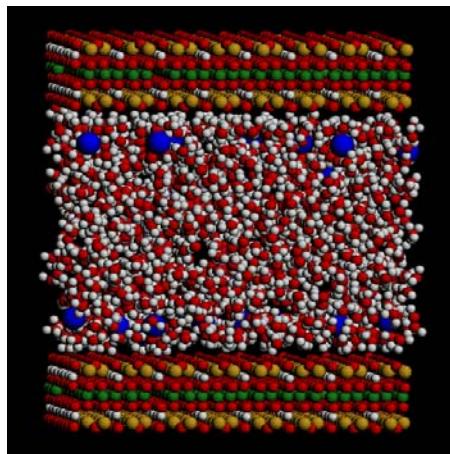
rheology
diagenesis

Small-strain stiffness: Contact-controlled

**coarse
grains**



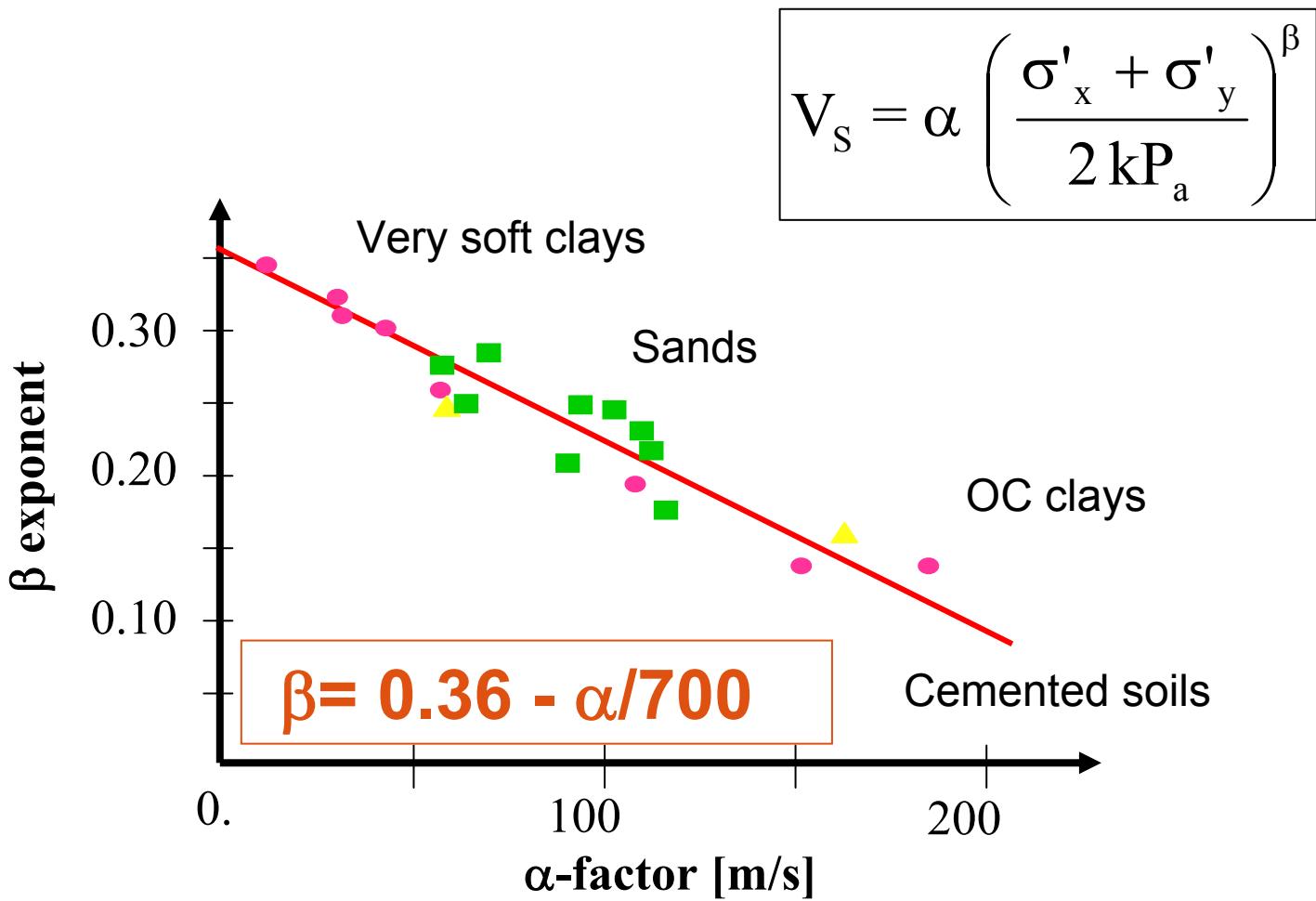
**fine
grains**



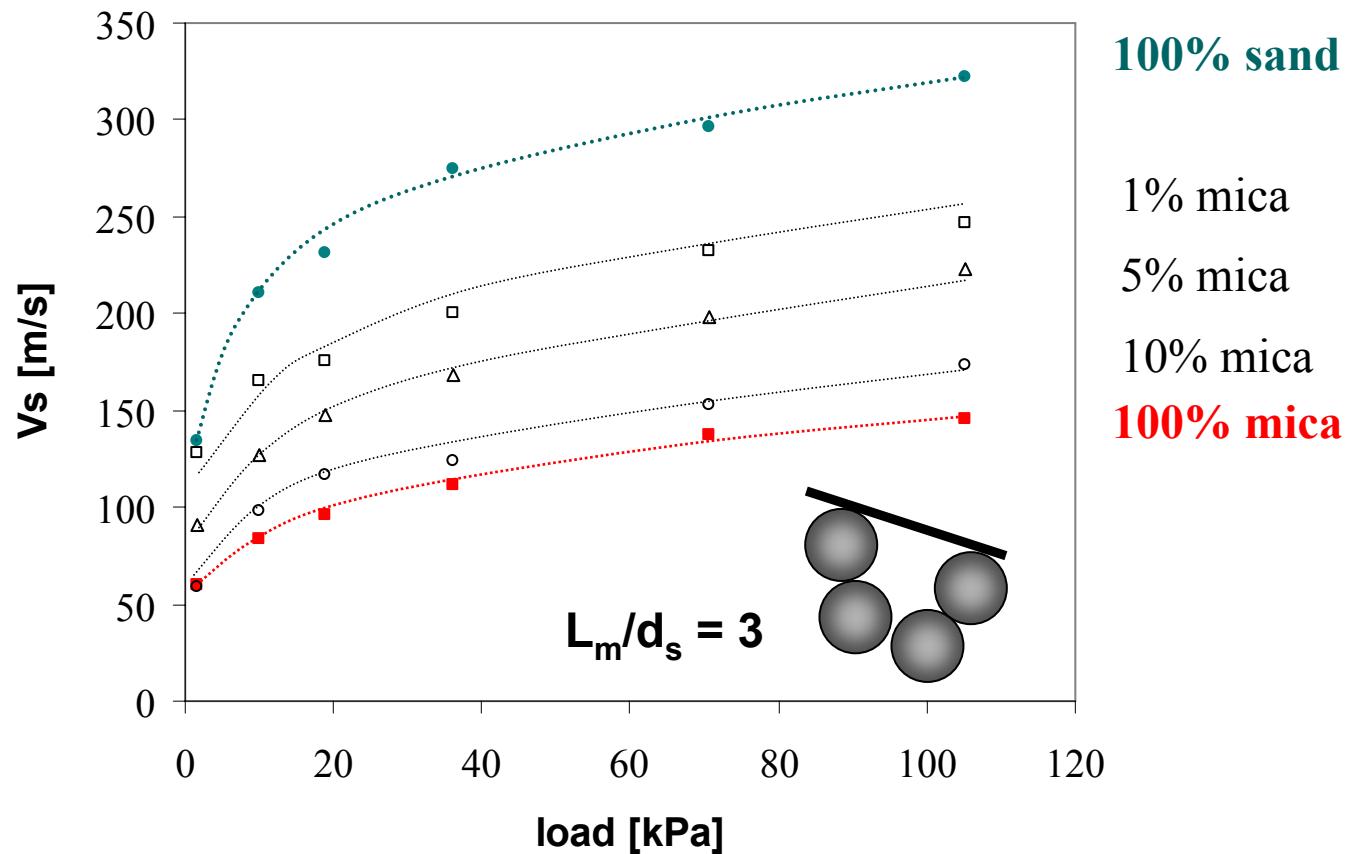
$$V_s = \alpha \left(\frac{\sigma'}{kP_a} \right)^{\beta} \quad \text{with } \beta = \frac{1}{6}$$

$$V_s = \alpha \left(\frac{\sigma'}{kP_a} \right)^{\beta} \quad \text{with } \beta < \frac{3}{4}$$

Stiffness-Stress: *contact behavior & fabric changes*



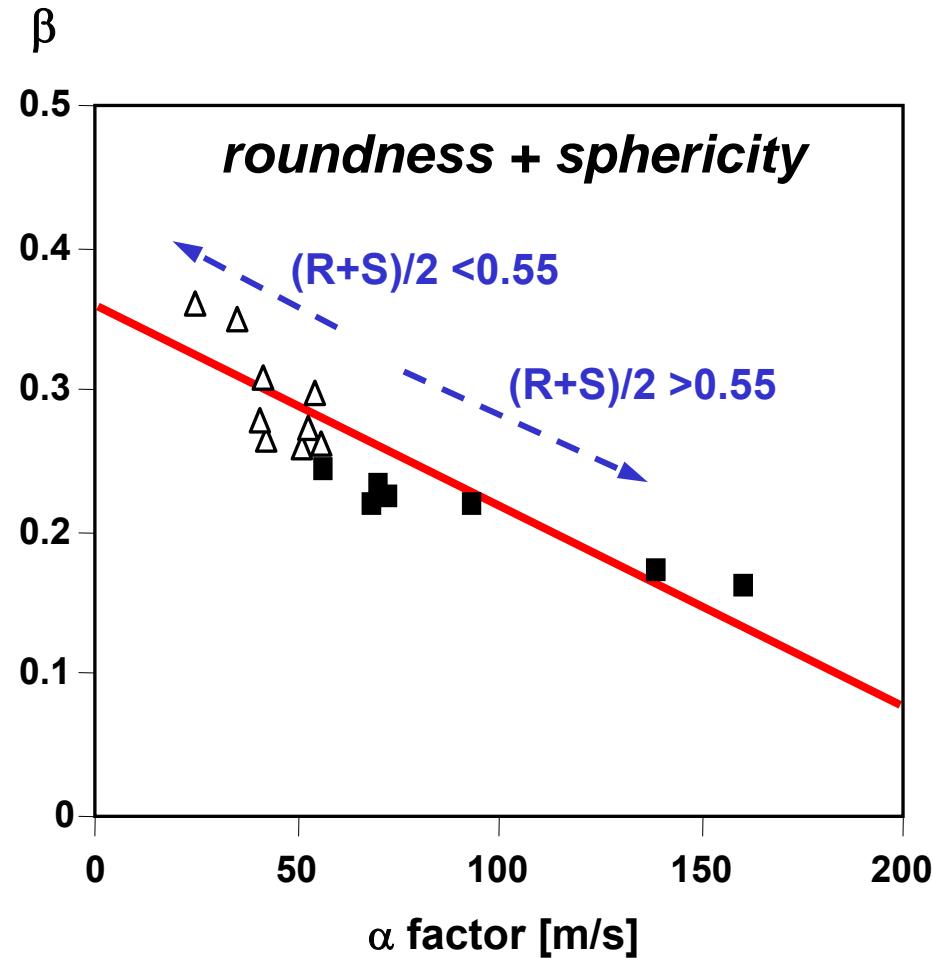
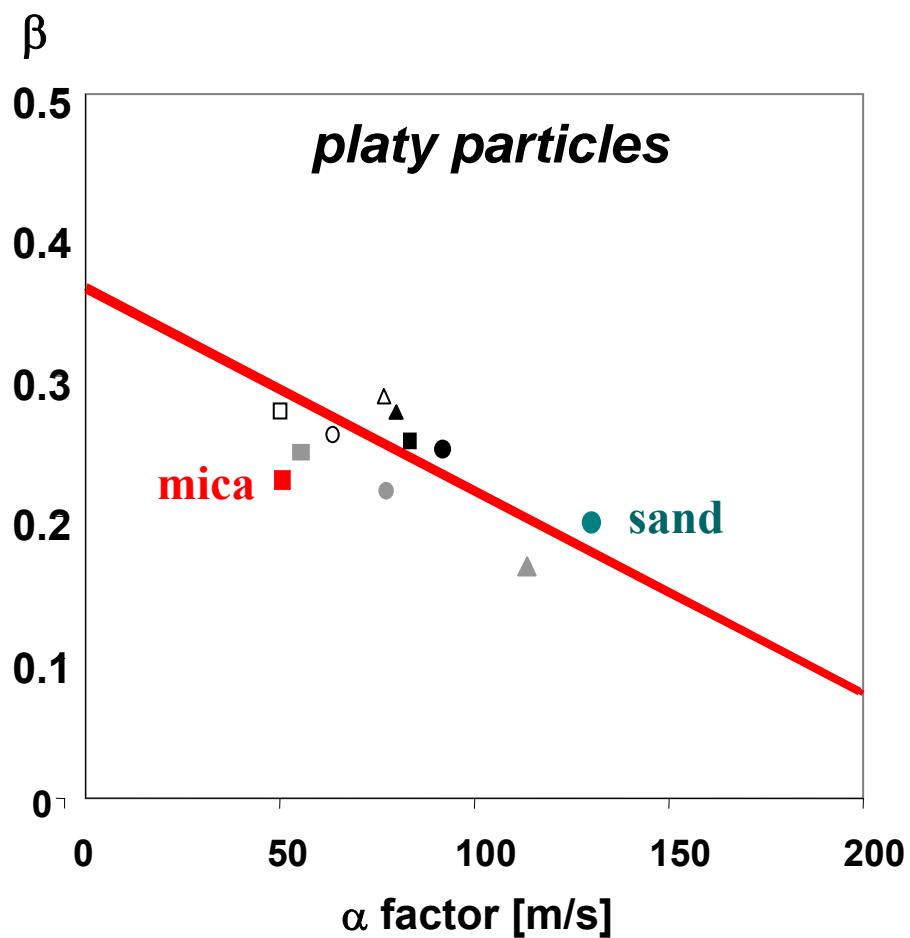
Stiffness: platy particles



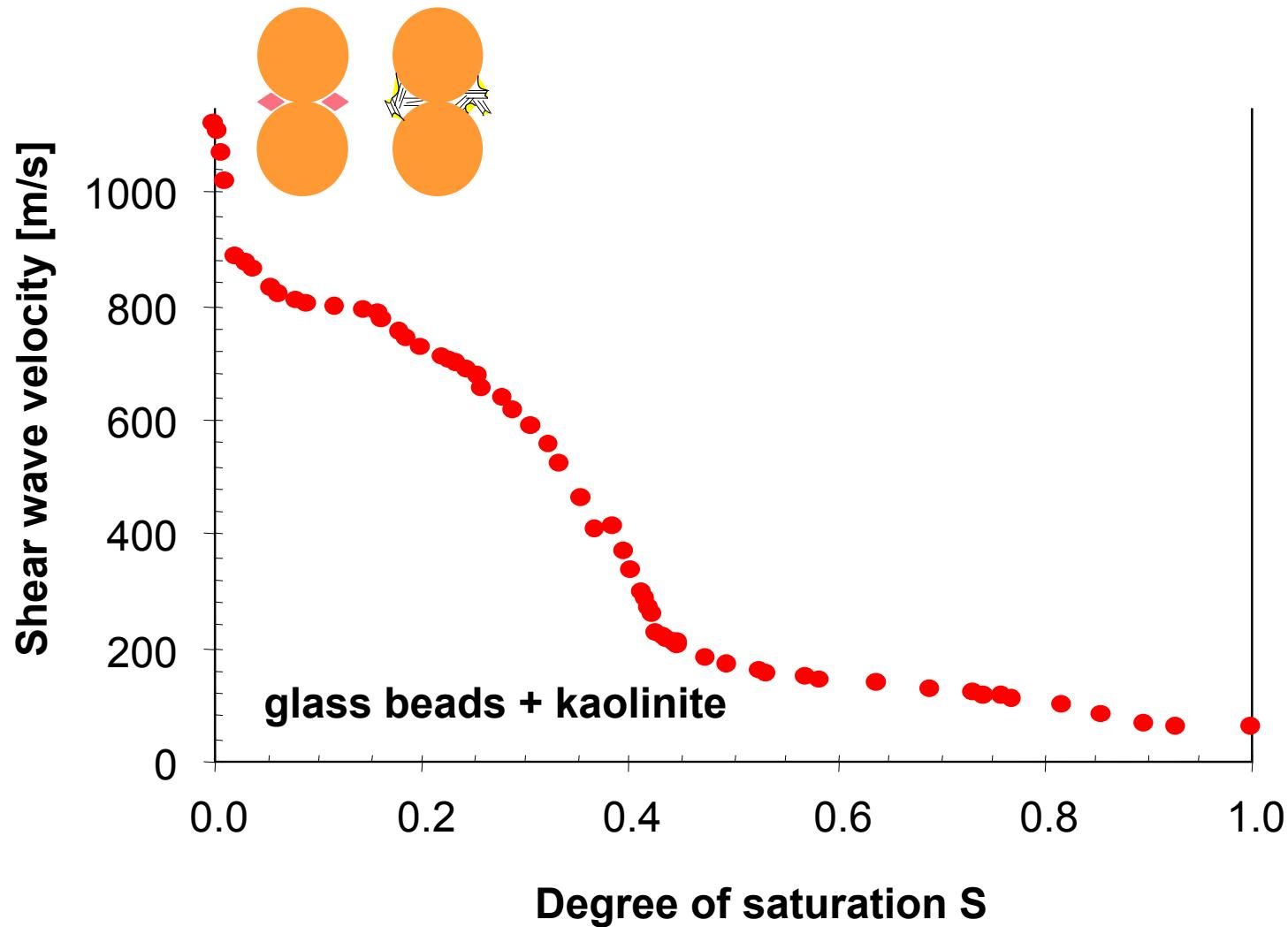
Particle shape effects

$$V_s = \alpha \left(\frac{\sigma'_x + \sigma'_y}{2 k P_a} \right)^\beta$$

$$\beta = 0.36 - \alpha / 700$$

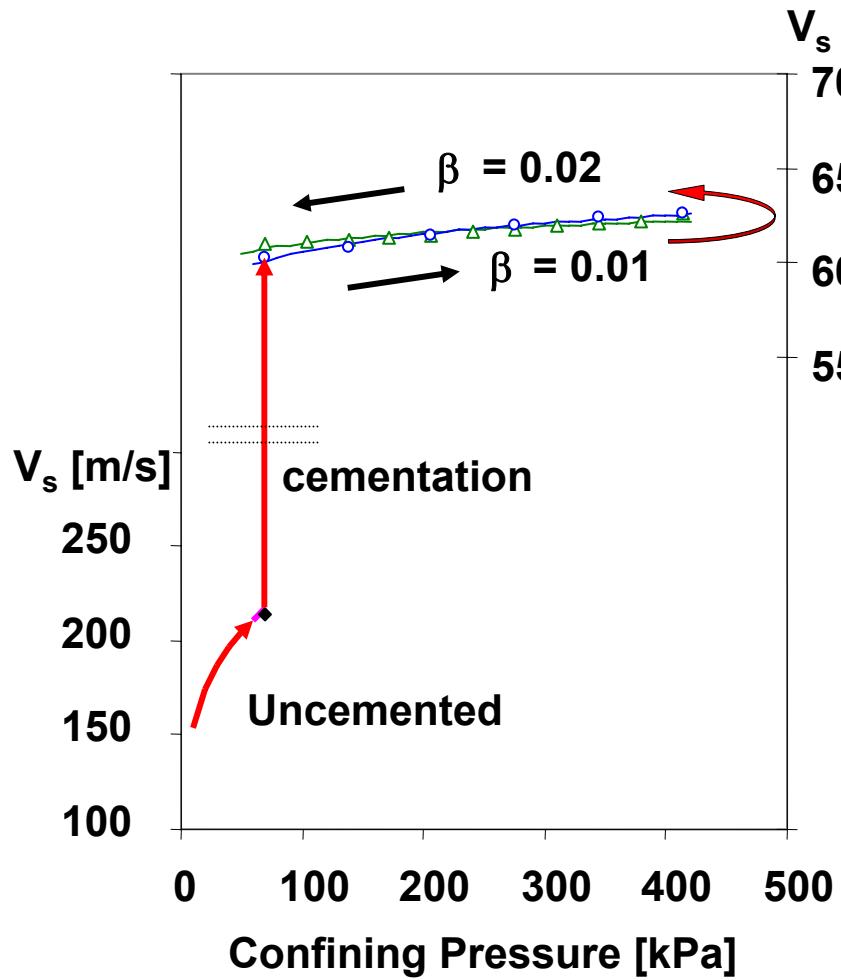


Drying – Unsaturated media

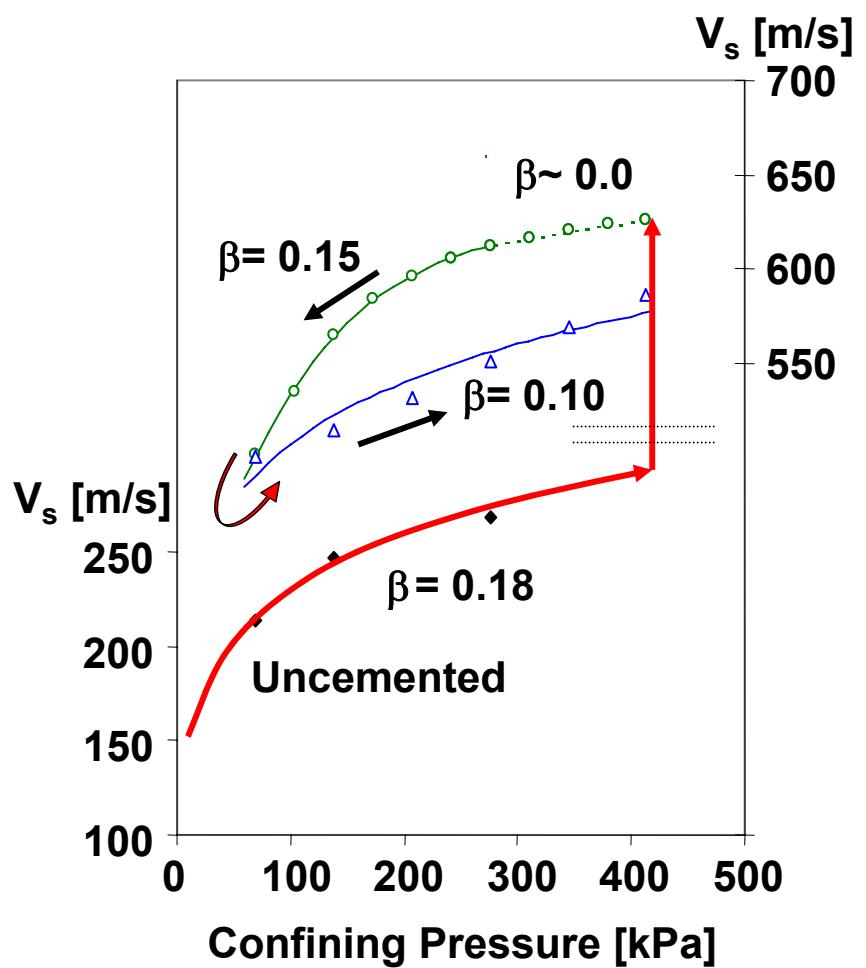


Stress change and cementation

Load (no unloading)



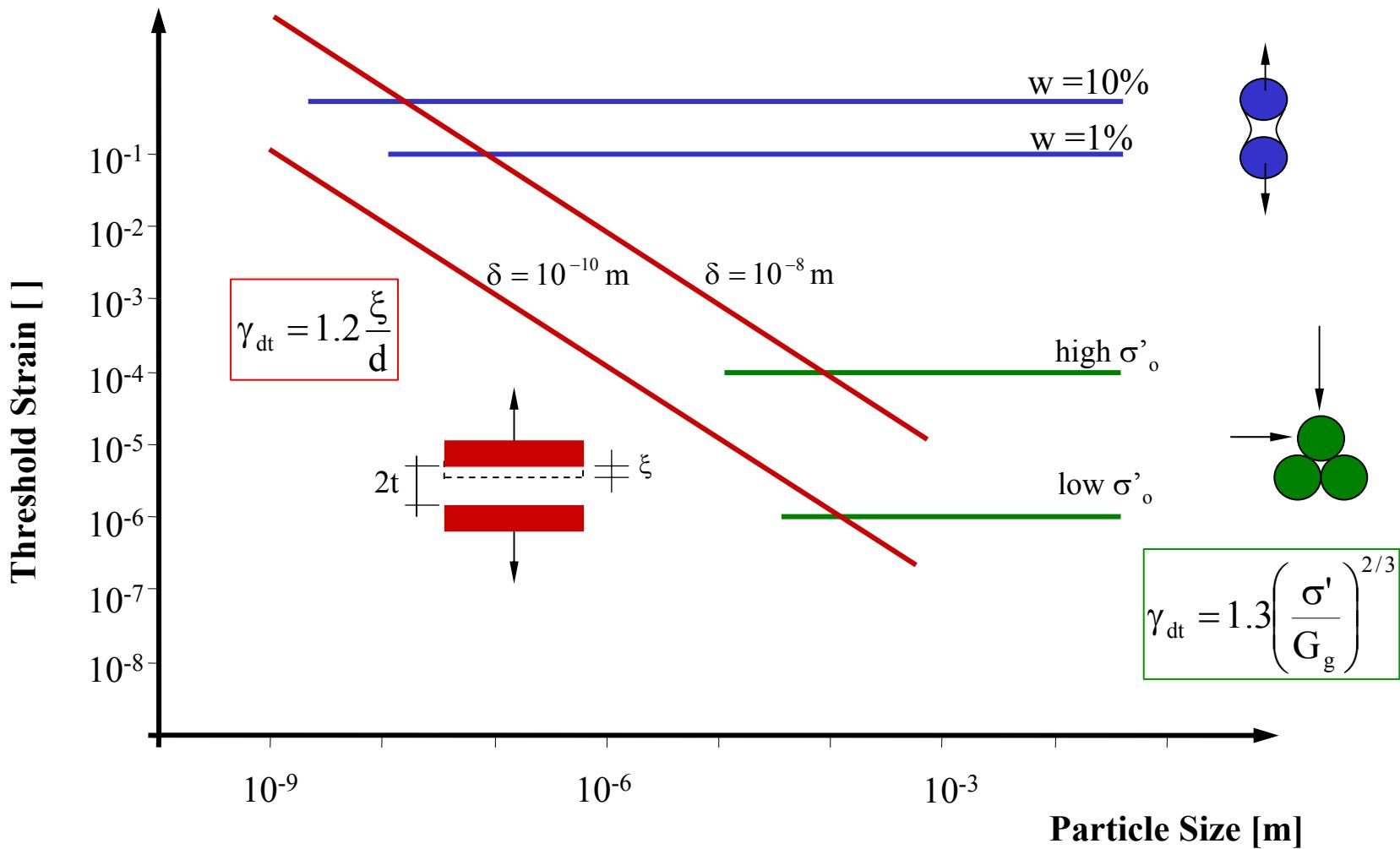
Unload and reload



Strain regimes

	<i>Small Strain</i>	<i>Large Strain</i>
Deformation	at contacts	fabric changes
Stiffness	maximum	decreases
Losses	very low	large - frictional
Volume Change	minimal	potentially large
Diagenetic effects	potentially high	small in drained shear
Fabric	constant	changes towards CS

Threshold strains - Ranges



fluid

particles

microorganisms

mineral

size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness

soil

fine-grained soil fabric
coarse-grained soil packing
platy particles

conduction
diffusion
energy coupling

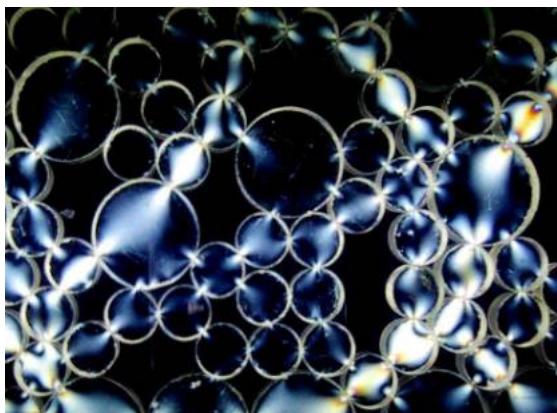
stiffness
threshold strain

strength
(scales)

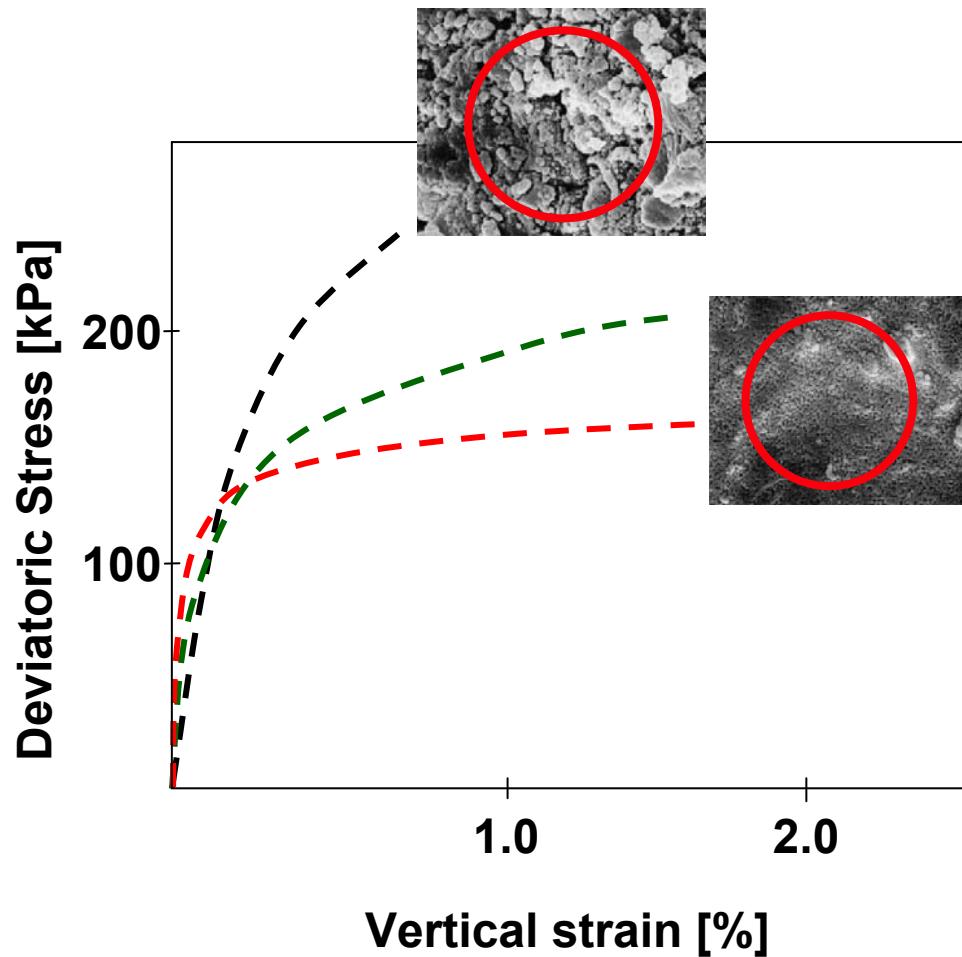
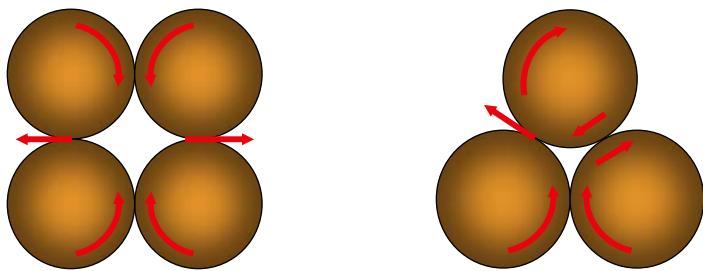
rheology
diagenesis

Stress-dependent strength and ε_{vol}

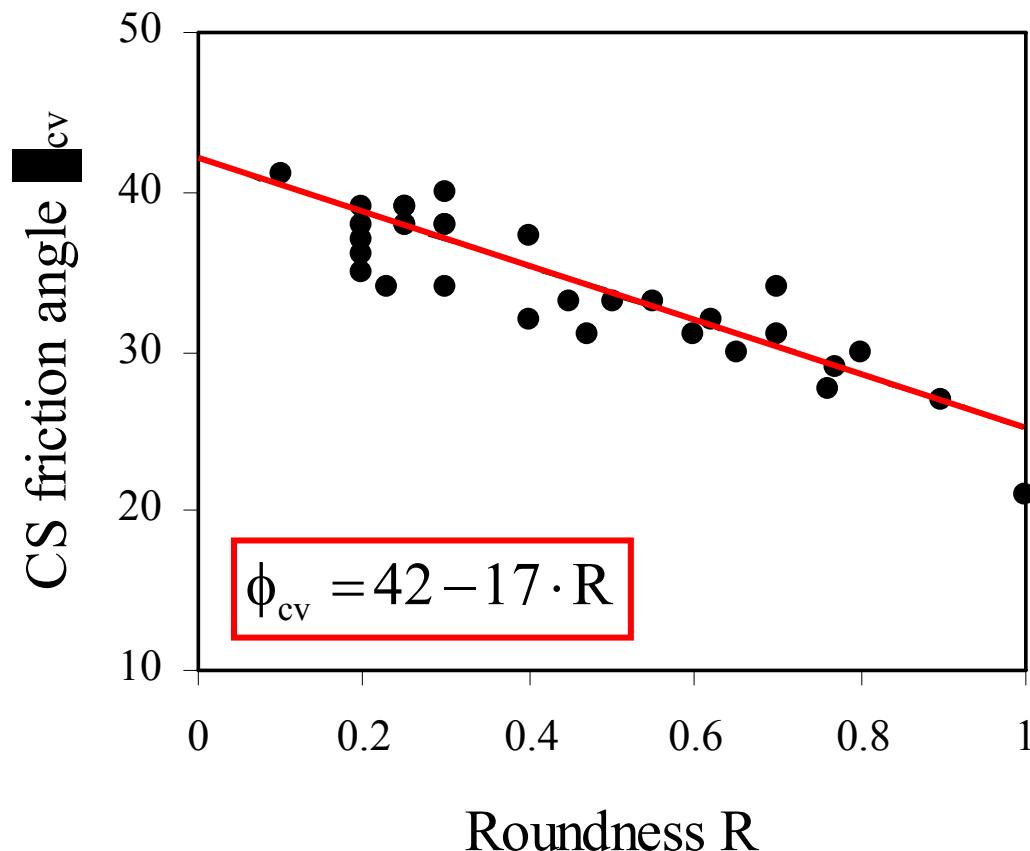
Chain buckling: coordination \uparrow



Rotational frustration:
coordination \downarrow



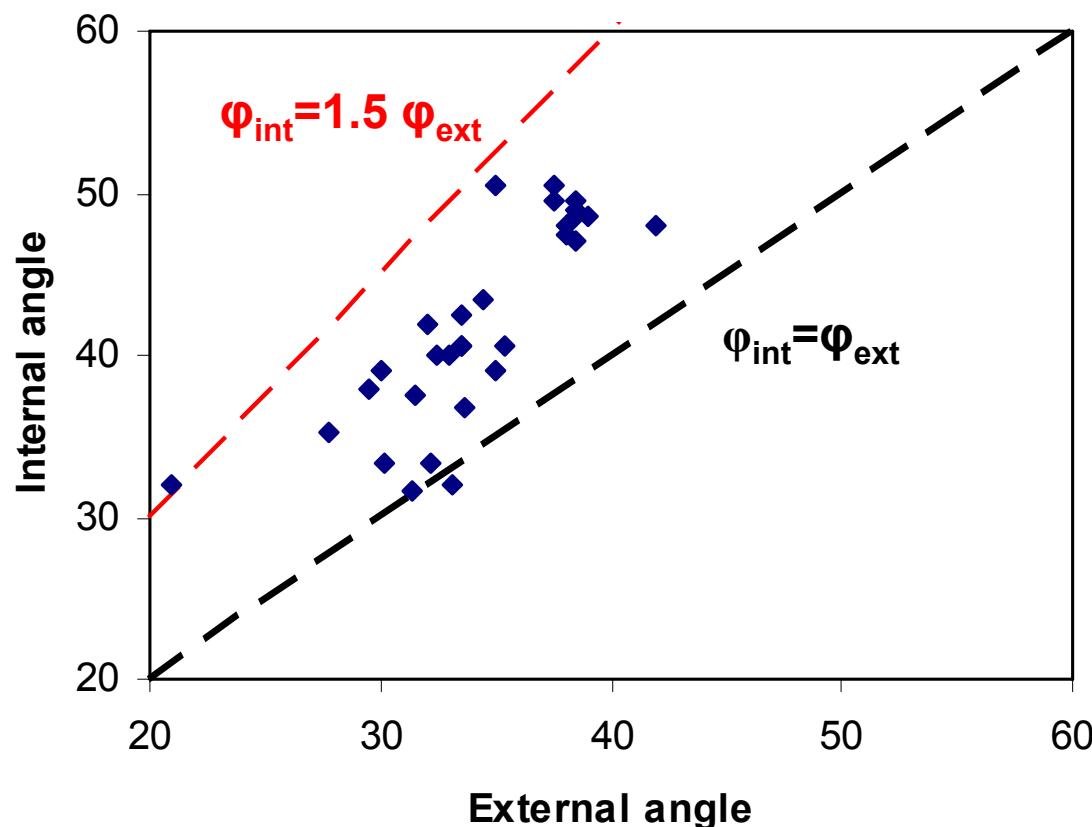
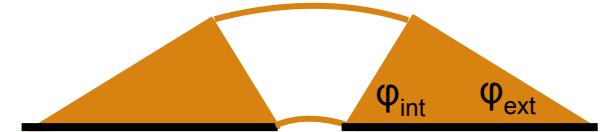
Effect of roundness on Φ_{cv}



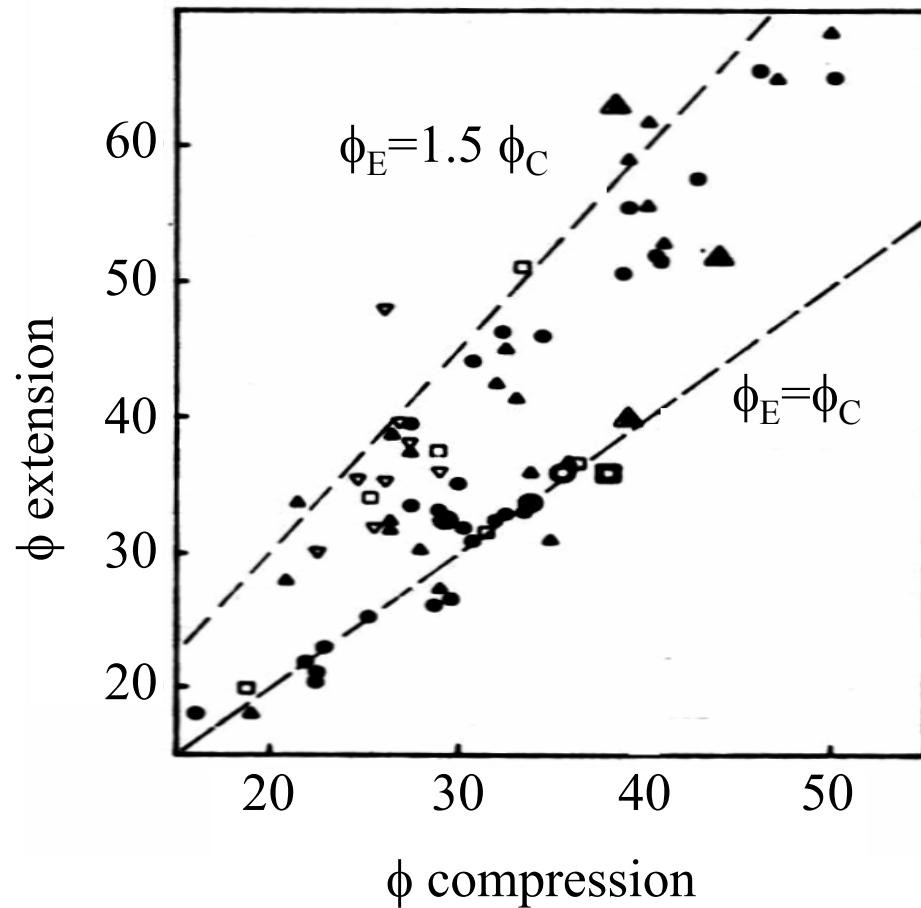
Evolution of internal micro-scale – 3D

		At peak dev. load	
Isotropic confine.		AC (b=0)	AE (b=1)
Contact normals			
$\underline{N}(\theta)$			
$\underline{T}(\theta)$ (magnified x5)	.		

Constant angle of repose?



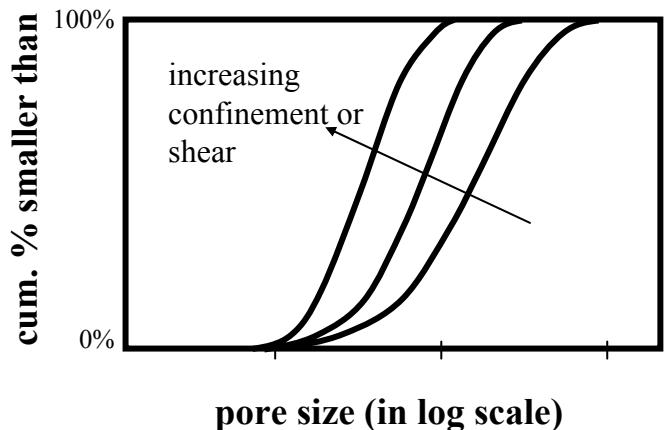
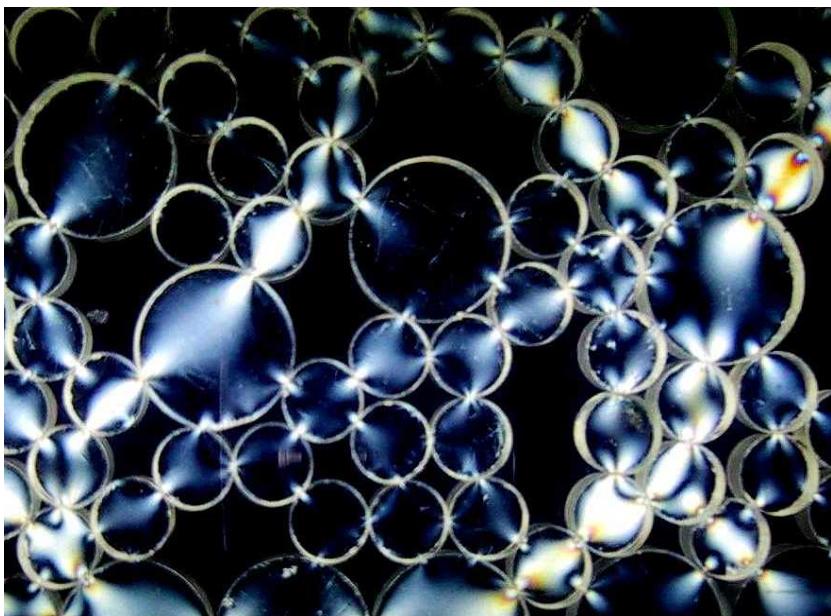
Anisotropy in ϕ - Clays



Undrained strength anisotropy

Controlled by the generation of pore pressure

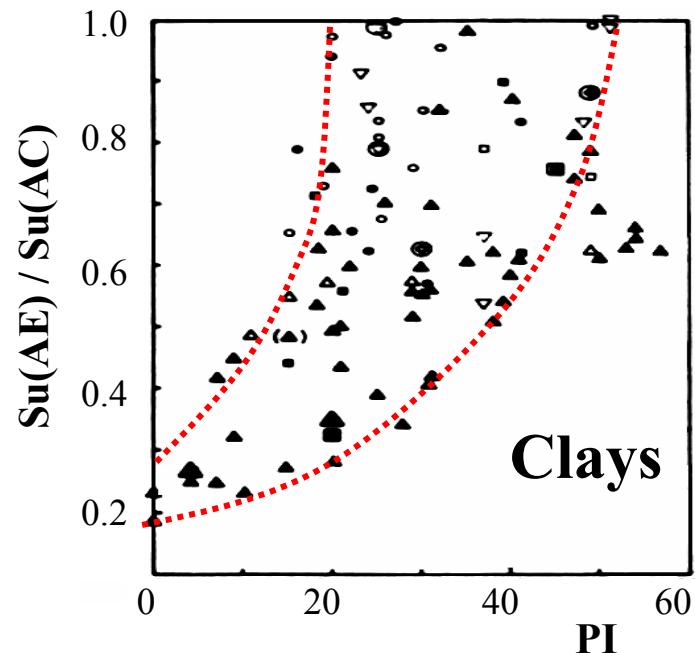
- *chain buckling and skeletal stiffness*
- *spatial variability of e*



Undrained strength anisotropy

Controlled by the generation of pore pressure

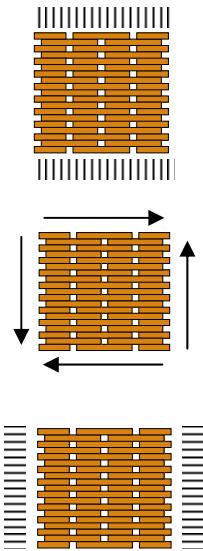
- *chain buckling and skeletal stiffness*
- *spatial variability of e*
- *threshold strain*



Undrained strength anisotropy

Controlled by the generation of pore pressure

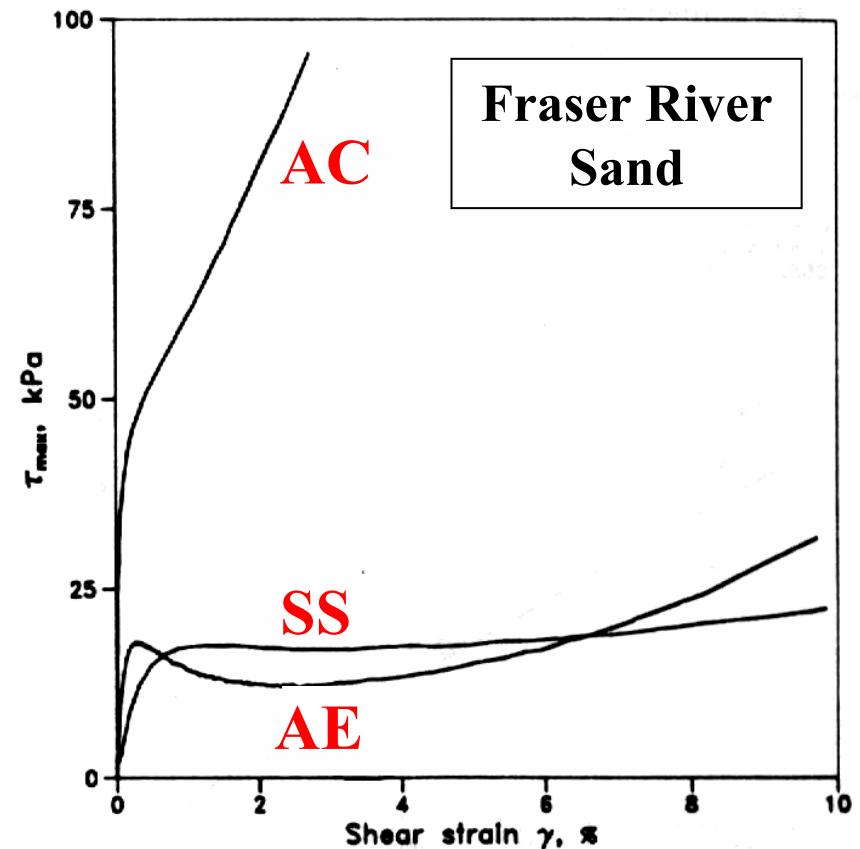
- *chain buckling and skeletal stiffness*
- *spatial variability of e*
- *threshold strain*
- *fabric anisotropy*



AC: $b=0 \ \alpha=0$

SS: $b>0 \ \alpha>0$

AE: $b=1 \ \alpha=90$



Scales

temporal

$$\frac{t_{\text{load}}}{L^2 / c_v}$$

$$\frac{f}{f_{\text{res}}}$$

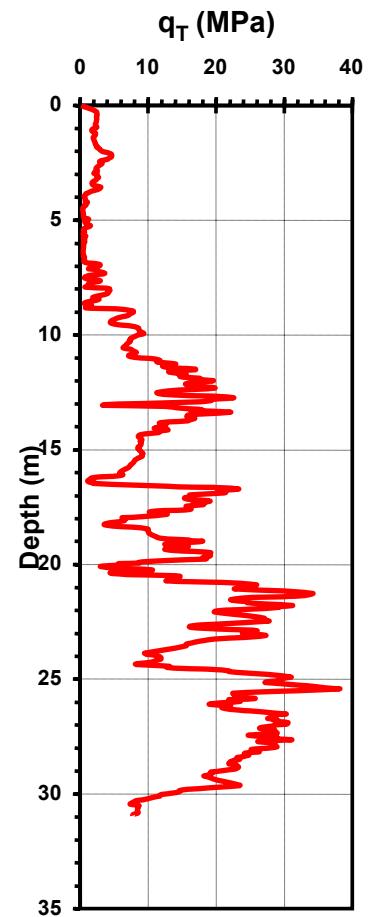
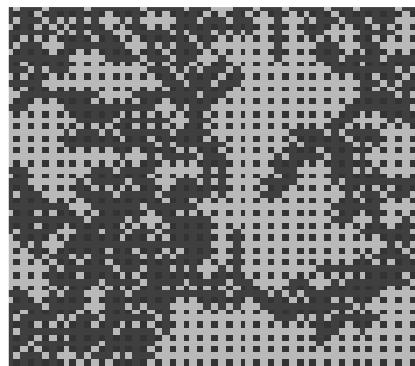
$$\frac{L / k_i}{L^2 / c_v}$$

*drained or
undrained*

*quasi-static
or dynamic*

*seepage or
consolidation*

spatial



fluid

particles

microorganisms

mineral

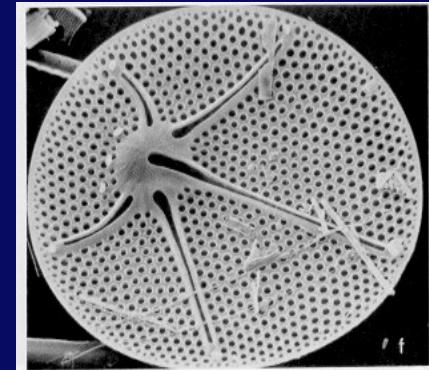
size

shape

surface charge
double layers
capillarity

forces
specific surface
relative size

sphericity
roundness
smoothness



soil

fine-grained soil fabric
coarse-grained soil packing
platy particles

conduction
diffusion
energy coupling

stiffness
threshold strain

strength
(scales)

rheology
diagenesis

			$C_u > 4, 1 \leq C_c \leq 3$	GW
COARSE	Gravel: $> 50\%$ retained sieve #4	$< 5\%$ fines	relative size else ...	GP
		$> 12\%$ fines	Below 'A' line	GM
			Above 'A' line	GC
	Sand: $< 50\%$ retained sieve #4	$< 5\%$ fines	$C_u > 6, 1 \leq C_c \leq 3$	SW
		filled porosity	else ...	SP
		$> 12\%$ fines	Below 'A' line	SM
			Above 'A' line	SC
FINE	$LL < 50$			ML
				CL
	$LL > 50$			OL
				MH

50-100 μm

plasticity index

liquid limit

mineral, S_s pore fluid

A line

CH

OL or MH

CL

OL or ML

CL

CL-ML

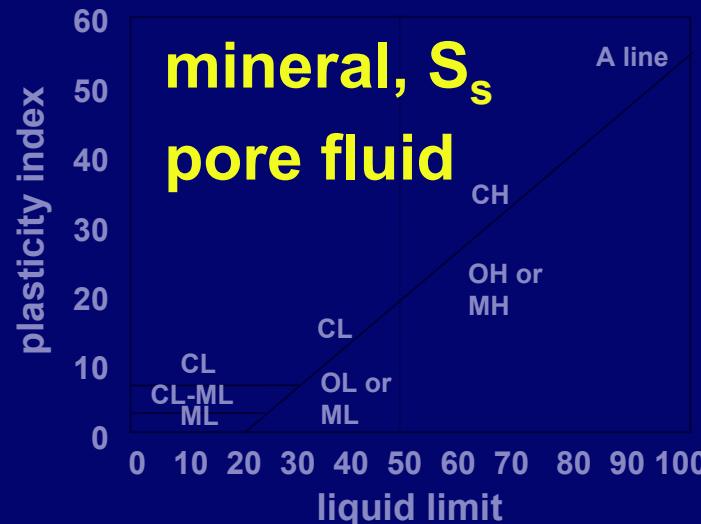
ML

OL

MH

CH

OH



			$C_u > 4, 1 \leq C_c \leq 3$	GW
			else ...	GP
			Below 'A' line	GM
			Above 'A' line	GC
			$C_u > 6, 1 \leq C_c \leq 3$	SW
			else ...	SP
			Below 'A' line	SM
			Above 'A' line	SC
				ML
				CL
				OL
				MH
				CH
				OH

pore fluid (explicitly)

Gravel: $< 5\% \text{ fines}$

COARSE sand: $< 12\% \text{ fines}$

sieve #4

degree of saturation

particle shape - coarse

$> 50\% \text{ retained}$

sieve #4

specific surface - fines (explicitly)

Sand: $< 5\% \text{ fines}$

$< 50\% \text{ retained}$

sieve #4

extent of diagenesis

FINE

$LL < 50$

spatial variability

$< 50\% \text{ retained}$

sieve #200

$LL > 50$

inherent anisotropy

bio-activity and bio-viability

plasticity index

liquid limit