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P-wave monitoring of hydrate-bearing sand during CH₄-CO₂ replacement

D. Nicolas Espinoza*, J. Carlos Santamarina

School of Civil and Environmental Engineering, Georgia Institute of Technology, 790 Atlantic Drive, Atlanta, GA 30332-0355, USA

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ABSTRACT

The replacement of methane for carbon dioxide in natural gas hydrate-bearing sediments is a promising technology in view of a more sustainable use of fossil fuels. While previous studies have shown successful CH_4-CO_2 replacement in hydrates, the mechanical response of hydrate-bearing sediments during CO_2 injection, CH_4-CO_2 replacement, and CH_4 production needs to be adequately understood in order to avert production problems such as borehole instability, sand production, and buckling of the casing. We take advantage of the characteristics of elastic mechanical wave propagation in sediments to monitor CH_4 hydrate-bearing sands before, during, and after CO_2 injection. Results show that CH_4-CO_2 replacement occurs without a loss of stiffness in the granular medium. This implies that CO_2 -flooded sandy reservoirs can remain mechanically stable during and after CH_4 gas production. On the other hand, dry CO_2 dissolves hydrate, and continued sediment flushing with dry CO_2 reduces the degree of hydrate saturation in the pore space, opens the pore throats, and weakens the granular skeleton. This phenomenon may cause a significant loss of strength near the injection points and regions subjected to high liquid CO_2 flow rate. The results of complimentary analyses show a decrease in bulk stiffness as water is displaced by liquid CO_2 , a stiffening of the granular skeleton during hydrate formation at contacts (diffusion limited), and the implications of water solubility in liquid CO_2 .

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1. Introduction

The simultaneous injection and geological entrapment of CO₂, along with enhanced hydrocarbon recovery may increase the efficiency and sustainability of fossil fuels. Examples of these combined processes are CO₂ enhanced oil recovery, and CO₂ enhanced coal bed methane recovery. In this study, we focus on CH₄–CO₂ hydrate replacement whereby methane is recovered from hydrate-bearing sediments with the concurrent entrapment of CO₂.

Published theoretical studies and laboratory-scale experiments have shown the successful release of CH_4 as a result of the replacement reaction caused by CO_2 injection (Hirohama et al., 1996; Kvamme et al., 2007; Lee et al., 2003; McGrail et al., 2007; Tegze et al., 2007). Pore scale phenomena include heat release and diffusion controlled reactions, dissolution of fluid phases, gas production, and porefluid volume expansion (note: a comprehensive review of phenomena relevant to CH_4-CO_2 replacement can be found in Jung et al. (2010)). The first reservoir-scale trial test has been planned for the Alaska North Slope in 2011 (DOE – project DE-NT0006553).

P-waves provide insight into the stiffness evolution of hydratebearing sediments. The stiffness evolution affects the mechanical

* Corresponding author. E-mail address: nicolas@ce.gatech.edu (D.N. Espinoza). stability of production wellbores and gas hydrate reservoirs. Pwave methods have been used to monitor CO_2 field injection tests (Arts et al., 2004; Daley et al., 2008; James et al., 1995; Spyros and Bruce, 1997; Spyros et al., 1995; Xue et al., 2006) and to assess CO_2 transport and saturation in laboratory experiments (Angeli et al., 2009; Lei and Xue, 2009; Sarout et al., 2009; Shi et al., 2007). In this study we use P-waves to monitor the evolution of CH₄ hydrate formation, CO_2 flooding, CH₄– CO_2 replacement, and final hydrate dissociation in sands. The properties of CO_2 and CH₄ are reviewed first. This is followed by the experimental study and complimentary analyses.

2. Review of CO₂ and CH₄ properties

The physical and chemical properties of CO₂ depend on pressure–temperature PT conditions. The critical point of CO₂ is at *P*=7.38 MPa and *T*=304.1 K. The density of liquid CO₂ is usually lower than that of water, but there may be a density reversal at high pressure, such as in deep-sea settings (at 277.15 K, $\rho_{CO_2} > 1035 \text{ kg/m}^3$ when pressure is above ~28 MPa). The bulk compressibility of liquid CO₂ is an order of magnitude higher than that of water (Span and Wagner, 1996). The most important properties of CO₂ relevant to transport-conduction processes are: (a) very low viscosity, typically 10 times lower than that of water ($\mu_{CO_2} = 10^{-4}$ Pa s at 10 MPa and 280 K – Fenghour et al., 1998); (b) high diffusivity of water into liquid CO₂ ($D \approx 2-20 \times 10^{-8} \text{ m}^2/\text{s}$ at

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Table 1

Physical and mechanical properties of hydrate-bearing sediment constituents. The following constants and equations are used to predict P-wave velocity for the multiphase fluid-sediment system using the Biot–Gassman equation (Eqs. (3) and (4)).

Phase	CO ₂	CH ₄	Water-brine	Ice	Gas Hydrate	Mineral
Physical properties						
Mass density, $ ho$ (kg/m ³)	CO ₂ EOS ^a	CH₄ Peng–Robinson EOS ^b	Correlation ^c	921 ^d	CH ₄ hyd: 930 ^e CO ₂ hyd: 1100 ^f	Quartz: 2650
Viscosity, μ (Pas)	Experimental fitting ^g	$2\pm0.5\times10^{-5}~h$	${\sim}1.5 \times 10^{-3~i}$	Does not apply	Does not apply	Does not apply
Mechanical properties						
P-wave velocity, $V_P(m/s)$	Correlation based on ^j	Polynomial equation ^k	Equation ¹	3870 ^d	3780 ^d	6060 ^m
S-wave velocity, $V_{\rm S}$ (m/s)	0	0	0	1949 ^d	1963 ^d	4110 ^m
Shear modulus, G (GPa)	0	0	0	3.45 ^d	3.2 ⁿ 3.54 ^d	45^{\dagger}
Bulk modulus, B (GPa)	$f(V_P, ho)^\dagger$	$f(V_{P}, ho)^{\dagger}$	$f(V_P, ho)^{\dagger}$	9.18 ^d	7.1 ^m 8.51 ^d	37†
Poisson ratio, v	~0.5	~0.5	~0.5	0.33 ^d	0.32 ^d	$\sim 0.08^{m}$

^a Duan and Sun (2003).

^b Peng–Robinson parameters: $T_c = 191.15$ K, $P_c = 4.641$ MPa, $\omega = 0.0115$.

^c Mavko et al. (2009).

^d 31 MPa effective stress and 273.15 K (Helgerud et al., 2009).

e Sloan and Koh (2008).

^f Aya et al. (1997).

^g Fenghour et al. (1998) and Vesovic et al. (1990).

^h At 298 K, 10-20 MPa (Bicher and Katz, 1943).

ⁱ Brine at 293 K (Netherton et al., 1977).

^j Span and Wagner (1996).

^k Trusler and Zarari (1992).

¹ Belogol'skii et al. (2002) and Mavko et al. (2009).

^m Gueguen and Palciauskas (1994).

† Computed value.

7–20 MPa and \sim 300 K – Espinoza and Santamarina, 2010), (c) significant solubility of water in liquid CO₂ (0.05 mol/kg at 10 MPa and 285 K – Spycher et al., 2003), and (f) high solubility of CO₂ in water (0.83 mol/kg at 6.6 MPa and 274 K in the presence of hydrate – Hashemi et al., 2006).

The critical point of CH₄ is at *P*=4.60 MPa and *T*=190.6 K, therefore, CH₄ does not form as a liquid phase in geological reservoir applications. The mass density of gas CH₄ can be approximated with a cubic equation of state (see parameters in Table 1 – Peng and Robinson, 1976). The mass density and viscosity of CH₄ are low at reservoir conditions when compared to water; for example, $\rho_{CH_4} = 232 \text{ kg/m}^3$ and $\mu_{CH_4} = 2.7 \times 10^{-5}$ Pa s at *P*=30 MPa and *T*=280 K (NIST, 2010).

Both, CO_2 and CH_4 can form gas hydrates at high pressure and low temperature. Water molecules form a polyhedral structure, which allows them to host the corresponding gas molecules (Sloan and Koh, 2008). Even though both CO_2 and CH_4 form hydrate structure I, their solubility in water, cage occupancy in the hydrate, and thermodynamic stability inside hydrate cages differ significantly (Adisasmito et al., 1991; Anderson et al., 2003; Servio and Englezos, 2001, 2002). Mixed CH_4 – CO_2 gas conditions cause a shift in stability boundaries which depends on the CH_4/CO_2 mass ratio (Adisasmito et al., 1991; Seo and Lee, 2001).

Gas hydrates form in the pore space of sediments at the bottom of the ocean and at great depths in permafrost where *PT* conditions are within the hydrate stability zone and CH_4 is abundant (Kvenvolden, 1988). The pore habit of hydrates in sediments has a large impact on the physical properties of hydrate-bearing sediments (e.g. pore filling, segregated lenses, and cementing – Waite et al., 2009).

3. Design of experiments

We use P-waves to assess the evolution of hydrate in sediments. We purposely localize hydrate growth at contacts by using a partially saturated sand pack, so that all of the water is found at interparticle menisci. Therefore, the granular medium acts as a "sensor" that amplifies the signature of the physical processes taking place at tens of thousands of grain contacts. In particular, sand grains work as Hertzian stiffness sensors that can reflect minor changes in contact conditions. Thus, compressive and shear wave velocities increase significantly even with small changes in hydrate saturation (note: hydrate nucleates on grain surfaces and grows into the pore in water saturated sediments; much lower changes in stiffness take place in this case).

3.1. Materials

Ottawa Sand #20/30 is the host sediment (round grains, $d_{50} = 0.72$ mm and $d_{60}/d_{10} = 1.2$, where d_x is the diameter for the *x*-percentile in the distribution – details in Cho et al. (2006)). Fluids include research purity CO₂ and CH₄ gases, and distilled water.

3.2. Apparatus

The tests are conducted within a high-pressure chamber equipped with multiple ports for fluid injection, electronics connections, and pressure measurement devices (transducer Omega PX303-GV). A sapphire window allows for direct observation into the pressure chamber. Inside the chamber, we place a springloaded sediment cell (25 mm diameter and \sim 20 mm height – Fig. 1) designed to apply a 100 kPa effective axial stress at zero lateral strain conditions. The cell is equipped with piezoelectric transducers (5 mm radius, 0.2 mm thickness) to generate and receive P-waves (Fig. 1). The piezoelectric transducers are connected to a signal generator BK PRECISION 4012A and an oscilloscope HP54600B. The input signal is a step function that repeats every 20 ms. The output signal is passed through a 300 kHz low-pass analogue filter and is sampled at 5 MHz. A total of 32 consecutive signals are averaged to increase the signal-to-noise ratio, and stored every 30s (note: we observe the waveforms on the oscilloscope screen continuously during critical processes). A thermocouple



Fig. 1. Experimental devices. The spring-loaded sediment cell is housed inside the pressure chamber (shown with a dashed line). The spring applies a constant effective axial stress $\sigma' \approx 100$ kPa to the sand. The piezoelectric transducers attached to the lower and upper plates of the cell are used to generate and measure the compressive P-waves. A thermocouple (bottom right corner in the cell) measures the sediment temperature.

(Copper Constantan, Conax Buffalo) placed inside the sediment cell measures the pore-fluid temperature within the sand specimen. The sediment cell is perforated (0.5 mm diameter holes) to retain the sand grains and but to allow the free flow of CH_4 and CO_2 .

3.3. Experimental procedure

The sand is mixed with distilled water, packed inside the sediment cell, and loaded to a constant effective axial stress. Then, we place the sediment cell inside the pressure chamber, briefly apply a partial vacuum, and flush the system with CH_4 gas at least five times in order to remove the air inside of the chamber and specimen pore space. Immediately after, we start to log pressure, temperature, and P-wave arrivals.

We run a total of seven multi-stage tests using the same sand, at the same effective stress, but with different initial values of water saturation. We subject each specimen to a pre-specified pressure-temperature PT time history to gain detailed information related to hydrate formation, CH₄-CO₂ replacement, and subsequent dissociation. Ice and hydrate formation PT paths are chosen to facilitate hydrate formation and to gain physical insight. The PT histories during CO₂ flooding represent two plausible scenarios: (a) flooding inside the CH₄ hydrate stability field is expected to be safer but slower, while (b) CO₂ gas injection coupled with depressurization may be quicker but may be accompanied by sediment compaction. PT paths that induce hydrate dissociation allow us to confirm PT conditions at phase transition for either CO₂ or CH₄ hydrate. Finally, successive CO₂ flushing is relevant to anticipate the response of hydrate-bearing sediments subjected to high CO₂ advection. Results are summarized in the following section.

4. Results

The main stages in the various PT time histories are shown in Fig. 2. Fig. 3 shows typical waveform cascades measured during the different stages. The dominant frequency of the transducer-sediment coupled system is in the ultrasonic regime and ranges from \sim 20 kHz (sand pack in air) to 150 kHz (cemented by ice or hydrate). Specific observations for each PT stage are summarized next.

4.1. Ice and hydrate formation

(a) Specimen cooling and ice formation at grain contacts (path a_1 in Fig. 2). Ice formation lasts from 30 to 350 s for water saturation $S_w = 0.045$ to 0.37 (exothermic-heat transport controlled).



Fig. 2. Pressure–temperature time histories. The arrows show the PT conditions followed in various tests, not necessarily in chronological order (letters match datasets in Fig. 3). Phase boundaries are shown for CH₄ and CO₂ hydrate, the liquid–vapor boundary for pure CO₂ and the water–ice boundary as a dashed line (equations in Jung et al. (2010)). Initially, we freeze the water in a CH₄ atmosphere (a₁) and then increase pressure by injecting CH₄ gas (a₂). We formed hydrate from ice to hydrate (b) and from liquid water (c). CO₂ injection is shown as loops, first CO₂ flooding (d), followed by liquid–gas–liquid CO₂ cycles (e). The CH₄–CO₂ replacement is sought during the first CO₂ flooding inside the CH₄ HSZ (d) or during the excursion outside the CH₄ hydrate stability field (g). We dissociate any hydrate during the final depressurization step (h).

A pronounced increase in stiffness accompanies ice formation (e.g. Fig. 3a, initial S_w = 0.045).

- (b) CH₄ hydrate formation from ice in an excess-CH₄ atmosphere (paths a_2 and b in Fig. 2). The ice-bearing sediment is pressurized with CH₄ (path a_2) and warmed outside of the ice stability field (path b). We observe that CH₄ hydrate nucleates as ice melts. While hydrate formation at each meniscus is CH₄ diffusion-limited, the volume average P-wave velocity remains higher than in the unfrozen sediment at all times (Fig. 3b is a continuation of Fig. 3a initial S_w =0.045). Hydrate continues growing for ~12 h and the sediment mixture continues to increase in stiffness (only 45 min shown in Fig. 3b).
- (c) CH₄ hydrate formation from water in an excess-CH₄ atmosphere (path c in Fig. 2). In this case, the initial sediment temperature is above that of the hydrate phase boundary, and the hydrate is formed by cooling (Fig. 3c). This process is much longer than ice formation because the growth is not governed by heat transfer but instead by the CH₄ diffusive transport through the hydrate layer that forms at the interface between the pendular water and the bulk CH₄ gas (for $S_w = 0.10$, ice formation takes place in less than 30 s, yet hydrate formation requires about 24 h). The duration of hydrate formation increases with the initial water saturation S_w .

4.2. CO₂ flooding

(d) CO_2 flooding and displacement of CH_4 (path d in Fig. 2). After CH_4 hydrate forms at grain contacts, we flood the pore space with gaseous, then, liquid CO_2 while the PT conditions remain within the CH_4 hydrate stability field. CH_4 is slowly vented while CO_2 is pumped into the chamber. The liquid phase formation is observed through the sapphire window; the interface rises to eventually fill the chamber as the injection of CO_2 continues. From PT conditions and bubble point data, we estimate that less than 10% of the methane remained in the chamber,



Fig. 3. P-wave measurements in hydrate-bearing sand (void ratio $e \sim 0.7$, effective confining stress $\sigma' \sim 100$ kPa, and mean particle size $d_{50} = 0.72$ mm). Waveforms from time-lapse P-wave monitoring: *x*-axis, oscilloscope time (μ s); *y*-axis, experimental time from the top to the bottom (min). Waveform voltage in colors, white denotes the signal peaks and black the signal troughs. Each frame represents a different process (results from various tests – refer to Fig. 2 and Section 3). Notice the high contrast in frequency and amplitude between water unsaturated and either ice or hydrate-bearing sediments. Notes: HPB hydrate phase boundary, * increased contrast to show low amplitude waveforms. Summary of PT histories for experiments shown in this figure: (1) initial $S_w = 0.045$ (a₁, a₂, b, d, e, and h); (2) initial $S_w = 0.10$ (a₁, a₂, b, f, c, d, h); and

mostly above the sediment cell (see CH₄–CO₂ phase equilibria in Donelly and Katz, 1954). Fig. 3d shows the results gathered during the liquid CO₂ flooding of a CH₄ hydrate-bearing sand at a hydrate saturation of $S_{hyd} \sim 0.045$; based on the evolution of P-wave velocity to an asymptotic value and on the time for diffusion-controlled growth (Section 5.3), we assume all water

(3) initial $S_w = 0.27$ (a_1 , a_2 , b, f, c, g, and final depressurization).

has converted to hydrate at this point. PT conditions remain within the CH₄ hydrate stability field. There is no significant stiffness change.

(e) Liquid–gas–liquid CO₂ cycle at $S_{hyd} \sim 0.045$ (path e in Fig. 2). We renew the CO₂ in the pore space by imposing a liquid–gas–liquid CO₂ cycle, to simulate extensive flushing of the sediment with

pure liquid CO₂. Fig. $3e_1$ shows the first of ten CO₂ flushing cycles. The wave velocity does not change significantly when the pore-fluid is changed from liquid CO₂ to gaseous CO₂.

(f) Liquid–gas–liquid CO₂ cycle at $S_{hyd} \ll 0.045$ (same as path e in Fig. 2). When hydrate saturation is very low, the difference in bulk stiffness when pores are filled with liquid CO₂, as opposed to gaseous CO₂, is evident (Fig. 3e₈): as soon as CO₂ vaporizes, the waveform shifts to having long travel time (~20 µs to >40 µs) and low frequency.

4.3. Hydrate dissociation

- (f) Dissociation of CH₄ hydrate (path f in Fig. 2). Fig. 3f shows CH₄ hydrate-bearing sand in CH₄ gas as it is heated beyond the hydrate stability field. The dissociation of CH₄ hydrate takes \sim 20 min for initial $S_{hyd} \sim 0.10$ (Fig. 3f). As soon as the specimen crosses the CH₄ hydrate dissociation boundary, the P-wave velocity starts to decrease. After complete dissociation, the effective stress acting on the granular skeleton dominates the sediment stiffness (note: Fig. 3c is a continuation of Fig. 3f).
- (g) Dissociation of CH₄ hydrate in the presence of CO₂ (path g in Fig. 2). In this experiment, we take a specimen of CH₄ hydratebearing sand in CH₄ gas beyond the CH₄ hydrate stability field and simultaneously inject CO₂ in order to reach the region bound by the CH₄ and CO₂ hydrate phase boundaries. Upon continued CO₂ injection, the CO₂ gas becomes liquid CO₂. From PT conditions and dew point data, we estimate that less than 10% methane stayed in the chamber, mostly above the sediment cell (see CH₄-CO₂ phase equilibria in Donelly and Katz (1954)). The P-wave velocity hardly changes during the process (Fig. 3g, *S_{hyd}* = 0.27, during the time shown and afterwards). We observe this "hydrate preservation behavior" at low hydrate saturation as well (*S_{hyd}* = 0.03 – not shown in Fig. 3).
- (h) Hydrate dissociation after CO₂ flooding (path h in Fig. 2). Fig. 3h shows the dissociation of originally pure CH₄ hydrate in sand $(S_{hyd} \sim 0.10) \sim 48$ h after the injection of liquid CO₂. During depressurization, the specimen goes through the CH₄ hydrate phase boundary first; but the P-wave velocity remains almost constant until the CO₂ hydrate phase boundary is reached. A rapid loss of stiffness occurs once the PT conditions are beyond the CO₂ hydrate stability field, and the sediment stiffness returns to the original water-wet condition. Complete dissociation lasts ~15 min.

4.4. CO₂ flushing

We flush the CO₂ in the sediment by imposing the CO₂ pressure cycles sketched as path e in Fig. 2. Fig. 4 shows the complete stiffness evolution for a hydrate-bearing sand ($S_{hyd} \sim 0.045$) subjected to ten CO₂ flushing cycles (note: this is a 35 day long experiment; ice formation, hydrate formation from ice, and CH₄ displacement by liquid CO₂ are shown for completeness). The granular skeleton stiffness decreases gradually with each CO₂ flushing cycle. The P-wave velocity at the eighth flushing cycle is the same as for the water-wet sand pack at 100 kPa. We dismantled the chamber and recovered only dry sand from the sediment cell.

5. Complimentary analyses and discussion

Earlier physico-chemical arguments at the lattice-scale suggested that a solid–liquid–solid transition is required for CH_4-CO_2 replacement (Jung et al., 2010). However, macroscale experimental results presented here show almost constant sediment stiffness during CH_4-CO_2 replacement. It is concluded that the solid–liquid–solid transition takes place locally at a scale small

enough that the sediment volume average properties remain unchanged. Clearly, hydrate dissolution in liquid CO_2 -saturated reservoirs will be accompanied by stiffness loss (e.g. near the injection well), while new hydrate formation in excess-water reservoirs will increase the sediment stiffness (typically in the far field of the injection well).

The following complimentary analyses permit extracting additional information from these experiments and provide an approach to assess changes in the geological formation.

5.1. Frequency effects

The piezoelectric transducers used in this study have a high resonant frequency in air. Once buried in the sand, the resonant frequency is strongly dependent on the sand stiffness and the sediment mass within the near field of the transducer. Assuming a parallel stiffness model, we can estimate the effective natural frequency of the coupled sand-transducer system f_c (underlying expressions in Bevlins (1979); an analogous analysis for buried bender elements can be found in Lee and Santamarina (2005)).

$$f_c \approx \frac{1}{2\pi} \sqrt{\frac{(70^2/3)(t/r)^3 (E_p/(1-\nu_p^2)) + \eta E_s}{[(t/r)\rho_p + \beta\rho_s]\pi r^2}}$$
(1)

where $\beta = 2$ (first mode of vibration) and $\eta \sim 1.6$ (Poulos and Davis, 1974) are geometry related factors, and E_p and v_p are the Young's modulus and Poisson's ratio of the transducer. The sediment stiffness E_s determines the resonant frequency of these buried, thin transducers (thickness much smaller than the radius, $t/r \ll 1$). Indeed, experimental results show that at an effective stress of $\sigma' \sim 100$ kPa, the dominant spectral frequency ranges from 20 kHz (sediment without ice or hydrate) to 150 kHz (sediment with ice or hydrate). These values are readily corroborated by time series shown in Fig. 3. In all cases, the wavelength λ is greater than 20 times the grain size d_{50} and satisfies the equivalent continuum assumption. The wavelength λ remains significantly shorter than the travel distance in all measurements.

The frequency content of P-waves in the sand saturated with liquid CO₂ (refer to Fig. 3) often exceeds Biot's characteristic frequency (Biot, 1956) for our experimental conditions ($\phi \sim 0.42$, $\mu_{\text{liquid CO}_2} \sim 10^{-4}$ Pa s, $\rho_{\text{liquid CO}_2} \sim 0.9 \text{ kg/m}^3$, and $\kappa \sim 10^{-12} \text{ m}^2$).

$$f_c = \frac{\phi\mu_{CO_2}}{2\pi\rho_{CO_2}\kappa} \sim 10 \text{ kHz}$$
(2)

The ratio between the high and low frequency P-wave velocity is \sim 1.07 (equation in Santamarina et al. (2001)) and has a minor effect in these results and analysis. In view of field applications, we continue the analysis of P-wave velocity for the low frequency regime.

5.2. P-wave velocity – changes during liquid CO₂ flooding

In the low-frequency regime, the mixture bulk compressibility B_{mix} can be estimated using the low frequency Biot–Gassman equation (Bourbie et al., 1987; Mavko et al., 2009), while the mixture mass density ρ_{mix} is computed as a volume average. The general expressions for the system under consideration are,

$$B_{mix} = B_{sk} + \left(1 - \frac{B_{sk}}{B_m}\right)^2 \left[\left(\frac{S_w}{B_w} + \frac{S_{CO_2}}{B_{CO_2}} + \frac{S_{CH_4}}{B_{CH_4}} + \frac{S_{hyd}}{B_{hyd}}\right)\phi + \frac{1 - \phi}{B_m} - \frac{B_{sk}}{B_m^2} \right]^{-1}$$
(3)

$$\rho_{mix} = \phi(S_w \rho_w + S_{CO_2} \rho_{CO_2} + S_{CH_4} \rho_{CH_4} + S_{hyd} \rho_{hyd}) + (1 - \phi)\rho_m \quad (4)$$

where ϕ is the sediment porosity and *S* is the relative saturation with subindeces *w* for water, CO₂, CH₄, and *hyd* for hydrate. A similar expression can be used for ice by replacing *S*_{hyd}, *B*_{hyd} and ρ_{hyd} with *S*_{ice}, *B*_{ice} and ρ_{ice} . The physical and mechanical properties of water, CO₂, CH₄ and solids (i.e., quartz, ice, and hydrate)



Fig. 4. Reduction of hydrate-bearing sand stiffness during successive flushes of pure liquid CO_2 , as liquid–gaseous–liquid CO_2 cycles inside the CH_4 hydrate stability field. The vertical axis represents the ratio between the P-wave velocity at experimental time *t* and the initial P-wave velocity at time *t*₀ before ice and hydrate formation. Each liquid–gas–liquid CO_2 cycle replaces 0.030 kg of pure CO_2 every ~3 days, which is equivalent to 8.5 times the pore space of the sand specimen. Note: (*) during the CO_2 liquid–gas–liquid cycles, we show the V_P ratio for the specimen in gas CO_2 to highlight the effect of cementing hydrate on the granular skeleton. The sand does not show any evidence of cementation after the 8th liquid–gas–liquid CO_2 cycle (28th day in the figure).

are summarized in Table 1; notice that the bulk stiffnesses sort as $B_m > B_{ice} > B_{hyd}$ (*m*: mineral). A proper equation of state is used for the fluid phase to account for variations in pressure and temperature (see Table 1).

Eq. (3) disregards the stiffening effect of capillary forces in mixed fluid conditions, such as water– CO_2 mixtures; this approximation is adequate for coarser sediments and/or high effective stress levels. If needed, the value of B_{sk} can be increased as a function of suction and saturation.

The constrained modulus of the skeleton M_{sk} can be determined from V_P measurements in gas saturated sands $M_{sk} = V_P^2 \rho_{sk}$. From the theory of elasticity, the bulk and shear modulus of the skeleton are $B_{sk} = 1/3[(1 + v_{sk})/(1 - v_{sk})]M_{sk}$ and $G_{sk} = [(1 - 2v_{sk})/(2 - 2v_{sk})]M_{sk}$, where the small strain Poisson's ratio for the granular skeleton is low $v_{sk} = 0.1$ (Santamarina et al., 2001). Knowing B_{mix} (Eq. (3)), G_{sk} and ρ_{mix} (Eq. (4)), the compressive wave velocity of the fluid saturated porous medium can be computed as,

$$V_P = \sqrt{\frac{B_{mix} + (4/3)G_{sk}}{\rho_{mix}}} \tag{5}$$

Fig. 5 shows the ratio β between the P-wave velocity predictions for the sediment saturated with a water-CO2 mixture $(S_w + S_{CO_2} = 1)$, and the same sediment saturated with water only $(S_w = 1)$. Values of β are shown as a function of CO₂ saturation for different skeletal stiffnesses V_{Psk}, fluid pressures, and porosities. Parameters used in each pane are selected to match the conditions in our experiments and other published studies; data are superimposed on the graphs. The β -ratio is always less than one because the P-wave velocity of liquid CO₂ ranges between \sim 300 m/s (7 MPa, 300 K) and 590 m/s (10 MPa, 280 K) as compared to that of water $V_{P-water} \sim 1500 \text{ m/s}$. The β -ratio is most sensitive to the stiffness of the skeleton B_{sk} and G_{sk} , and it tends to $\beta = 1$ as the stiffness of the skeleton increases. The β ratio changes significantly with PT conditions and CO₂ saturation S_{CO_2} . Similar trends apply to brine-saturated media (P = 10 MPa; $T = \bar{2}80 \text{ K}; S = 10\%; B_w = 2.11 \text{ GPa}; B_{\text{brine}} = 2.64 \text{ GPa}; \rho_w = 1004 \text{ kg/m}^3;$ $\rho_{\rm brine} = 1075 \, \rm kg/m^3$).

An immediate implication of this analysis is that the injection of liquid CO₂ into water-saturated sediment in the field replaces high bulk stiffness water for the more compressible liquid CO₂ and a lower P-wave velocity is anticipated. Also we note that due to the low P-wave velocities of gas CH₄ and both gas and liquid CO₂ compared to the P-wave velocity of the hydrate-bearing sand $(V_P \sim 900 \text{ m/s} \text{ at } 100 \text{ kPa}$ vertical effective stress), P-wave velocities measured in this study closely track the evolution of skeletal stiffness. While the forward prediction of V_P is viable, flat trends in Fig. 5 indicate that the estimation of CO_2 saturation from V_P measurements will be inaccurate, especially in stiff, low porosity sediments where marked changes in CO_2 saturation have almost no impact on V_P .

5.3. Time evolution: formation rate

Diffusion controlled hydrate growth is anticipated at menisci (excess-gas conditions). CH₄ hydrate formation is limited by methane gas transfer through the hydrate layer thickness *s* that forms around the menisci (excess-gas sediment). At steady state, the flux of gas F_g from the pore space (concentration C_{bulk}) to the water inside the meniscus (concentration C_{ag}) is

$$F_g = D \frac{C_{bulk} - C_{aq}}{s} \tag{6}$$

where *D* is the diffusivity of CH₄ through CH₄ hydrate. The concentrations $C_{bulk} = \rho_{CH_4} \mod/L$ and C_{aq} depend on pressure and temperature conditions (Servio and Englezos, 2002; Servio et al., 1999). The gas concentration in hydrate is $C_{hyd} = 7.3$ in mol/L (full occupancy n = 5.75; lattice size 12 Å). For a quasi cylindrical geometry, the evolution of the hydrate shell thickness in time becomes,

$$s = \sqrt{2D \frac{C_{bulk} - C_{aq}}{C_{hyd} - C_{aq}} t}$$
(7)

We estimate the time required for hydrate formation t_{form} in pendular water at interparticle menisci by combining Eqs. (6) and (7), and substituting *s* for r_m ,

$$t_{form} = \frac{1}{8D} \frac{C_{hyd} - C_{aq}}{C_{bulk} - C_{aq}} d_{50}^2 \sqrt{S_w^{init}e}$$
(8)

Experimental diffusion values $D=3.4-7.6 \times 10^{-13} \text{ m}^2/\text{s}$ (Davies et al., 2008), combined with Eq. (8) lead to the conclusion that water in submillimetric menisci converts to hydrate in few days. Similar rates are expected to happen in diffusion controlled CH₄-CO₂ replacement processes.

5.4. Water solubility in liquid CO₂ and hydrate dissolution

Both CO₂ and CH₄ hydrates tend to dissolve in liquid CO₂ that is not water saturated, as confirmed by the results shown in Fig. 4 (see also Jung et al., 2010). An estimated \sim 30 mg of water could be dissolved into liquid CO₂ given the void space in our chamber under the experimental conditions in this study. Alternatively, only \sim 3 mg of water can dissolve into the CO₂-filled pore space of the sediment cell. The experiment shown in Fig. 4 starts with 180 mg of water in the sediment; i.e., S_w = 0.045. Thus, \sim 180 mg/30 mg = 6 to



Fig. 5. Ratio of compressive P-wave velocities for liquid and supercritical CO_2 -water saturated sediment and the same sediment saturated with water as a function of CO_2 saturation. The effects of (a) skeletal stiffness as represented in V_{Psk} ; (b) pore-fluid pressure P; (c) temperature T; (d) porosity ϕ . The bulk modulus and density of CO_2 , and water are calculated with equations of state as a function of pressure and temperature (Table 1). Laboratory and field results are superimposed.

180 mg/3 mg = 60 flushing cycles of CO_2 are needed to dissolve all hydrate-forming water into the surrounding liquid CO_2 . Nine CO_2 flushing cycles were sufficient in the experiment documented in Fig. 4.

6. Conclusions

CH₄-CO₂ replacement in hydrate-bearing sediments presents a unique opportunity to address increasing energy demands within the context of climate change. Considerable research efforts are needed to understand the complexity of underlying processes leading to commercial scale technological developments.

We designed an experiment that takes advantage of the contact-dependent sand stiffness to follow CH_4 hydrate formation, CO_2 flooding and gas replacement, and subsequent hydrate dissociation. The test design amplifies the process signatures by simultaneously measuring phase reactions that take place at thousands of interparticle menisci.

Hydrate growth in excess-gas sediments is controlled by CH₄ diffusion through the intermediate hydrate shell that separates bulk gas and free water.

After CO_2 flooding, the hydrate mass dissociates at the CO_2 hydrate dissociation boundary, which confirms the successful CH_4 – CO_2 replacement.

The hydrate-bearing sediment retains its stiffness during CO_2 flooding and gas replacement. Therefore, while a lattice-scale solid–liquid–solid transition is required for CH_4 – CO_2 replacement, the reaction is local and does not cause an appreciable effect on the macroscale mechanical properties of the hydrate bearing sediment.

The mutual solubility and diffusivity of water, CO_2 , and CH_4 components play a crucial role in the process of CH_4 – CO_2 replacement. Liquid CO_2 will dry water from the existing hydrate, causing a decrease in both hydrate saturation and sediment stiffness in regions subjected to extensive CO_2 flow, such as near the injection wells. This may lead to volume contraction, trigger borehole instability, and facilitate sand production.

The bulk modulus of CO_2 at reservoir conditions is lower than that of water. Therefore, P-wave velocity decreases as CO_2 displaces water from the pore space. The change in P-wave velocity is small in hard rocks and stiff sediments. This observation limits the use of P-wave monitoring of CO_2 injection.

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